

The morphology and evolution of Star Forming Regions & Binary Stars

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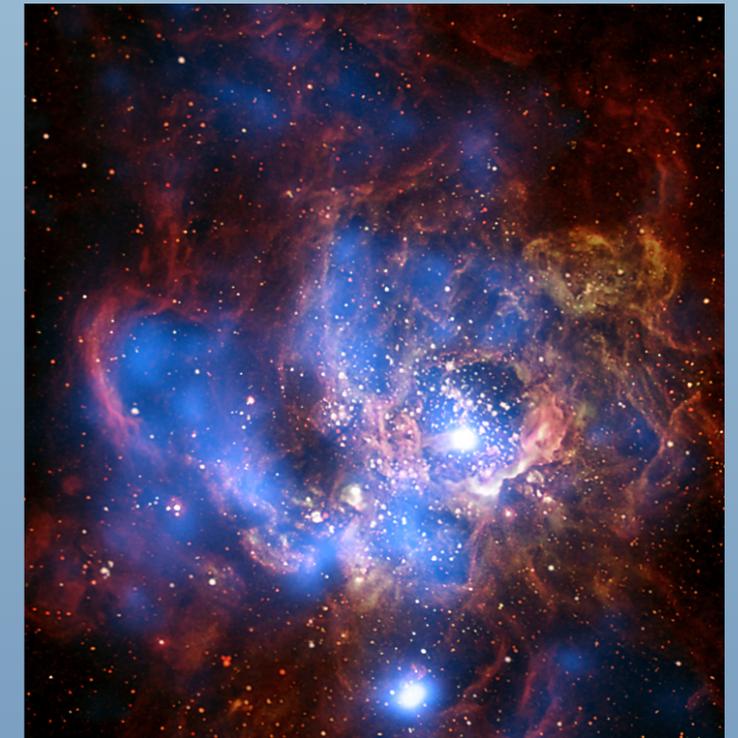
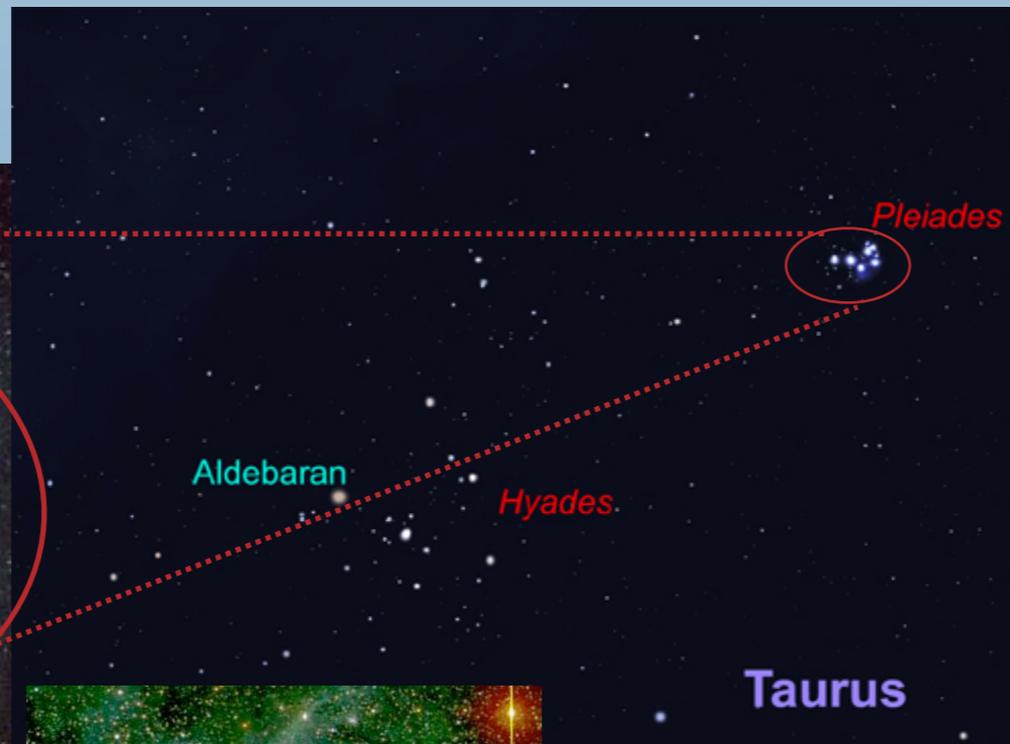
J. Dorval, Strassburg (PhD)

+

V. Niederhorn, Strassburg (MSc), H. Cromley (JHU), T. Kovacs (Budapest)

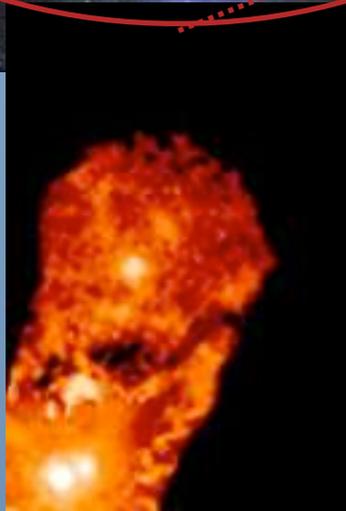
Aarseth meeting / Prague Czech Rep / December 12-15 2017

Observations ..



NGC604 in M33

Orion



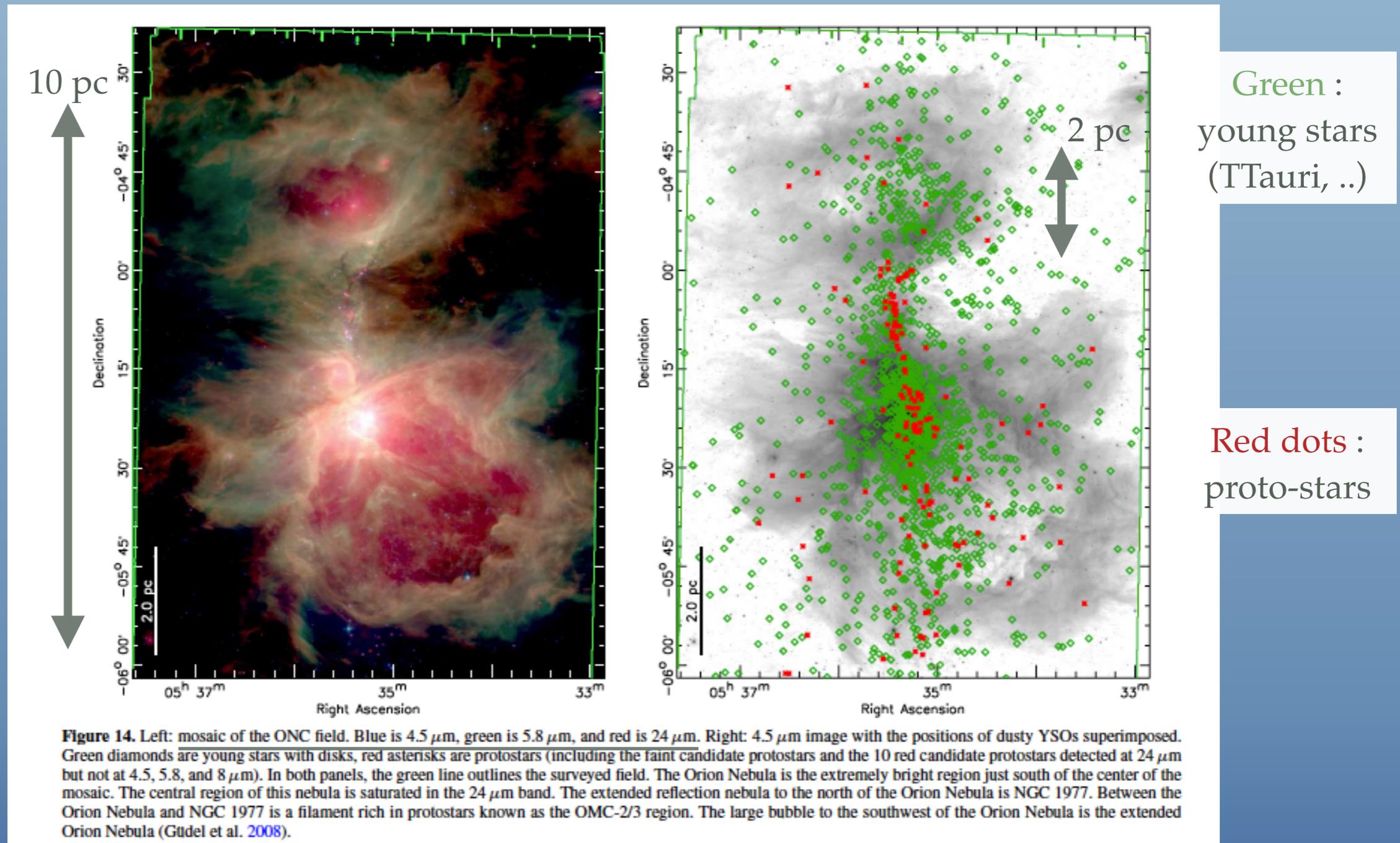
Wide range of star forming regions:

- $\rho \approx 10^1 - 10^7 M_{\text{Sun}} / \text{pc}^3$
- $M_{\text{cloud}} 10 \text{ to } \approx \text{few} \times 10^6 M_{\odot}$
- $\sigma \approx 30 \text{ km/s @ } 1 \text{ pc}$

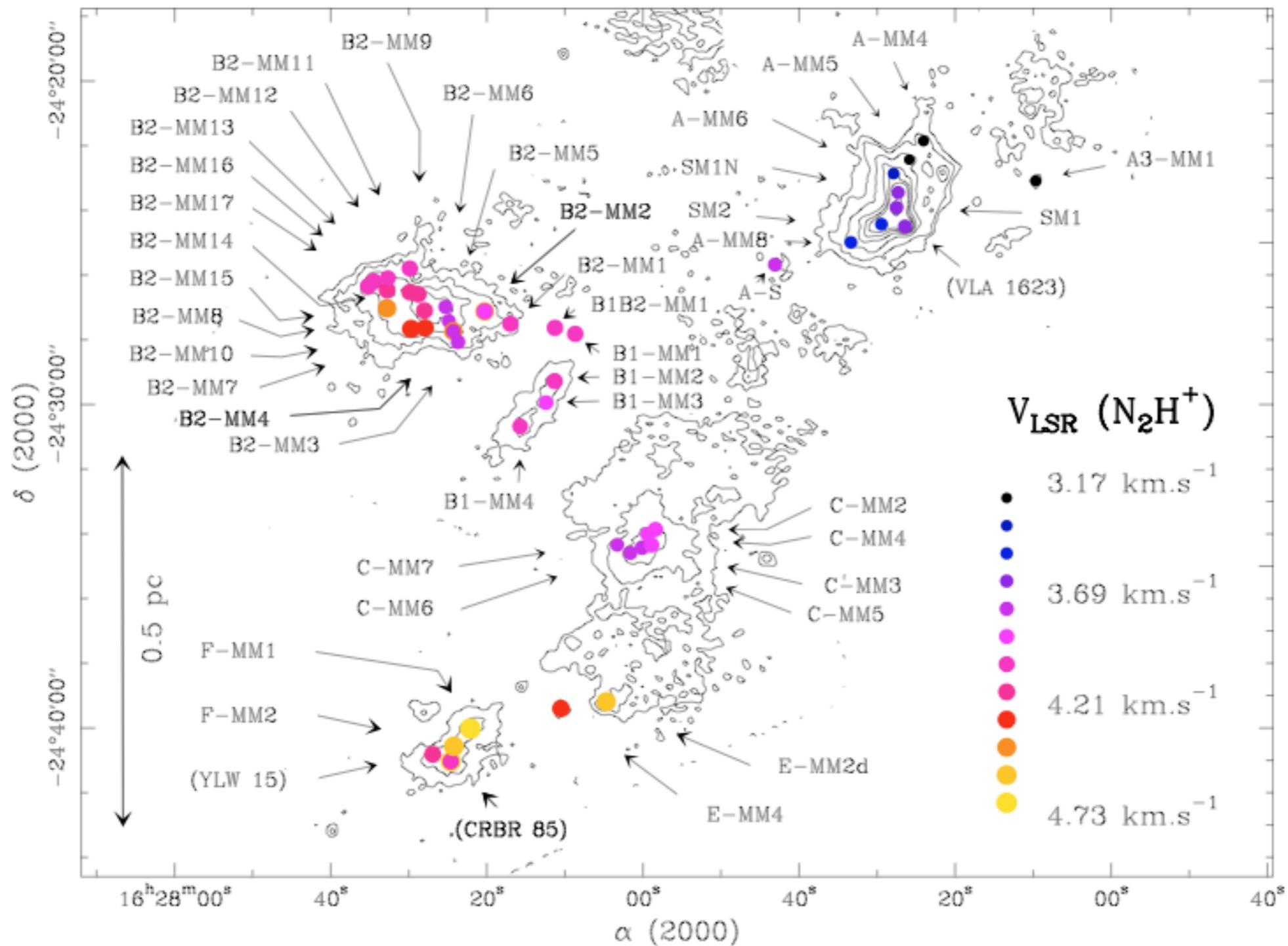
Credits: image lifted from NASA / PotD ++

Zoom-in : Spitzer IR data

Exemple: the ONC star-forming region



Credits : S. T. Megeath et al. 2012, 2015



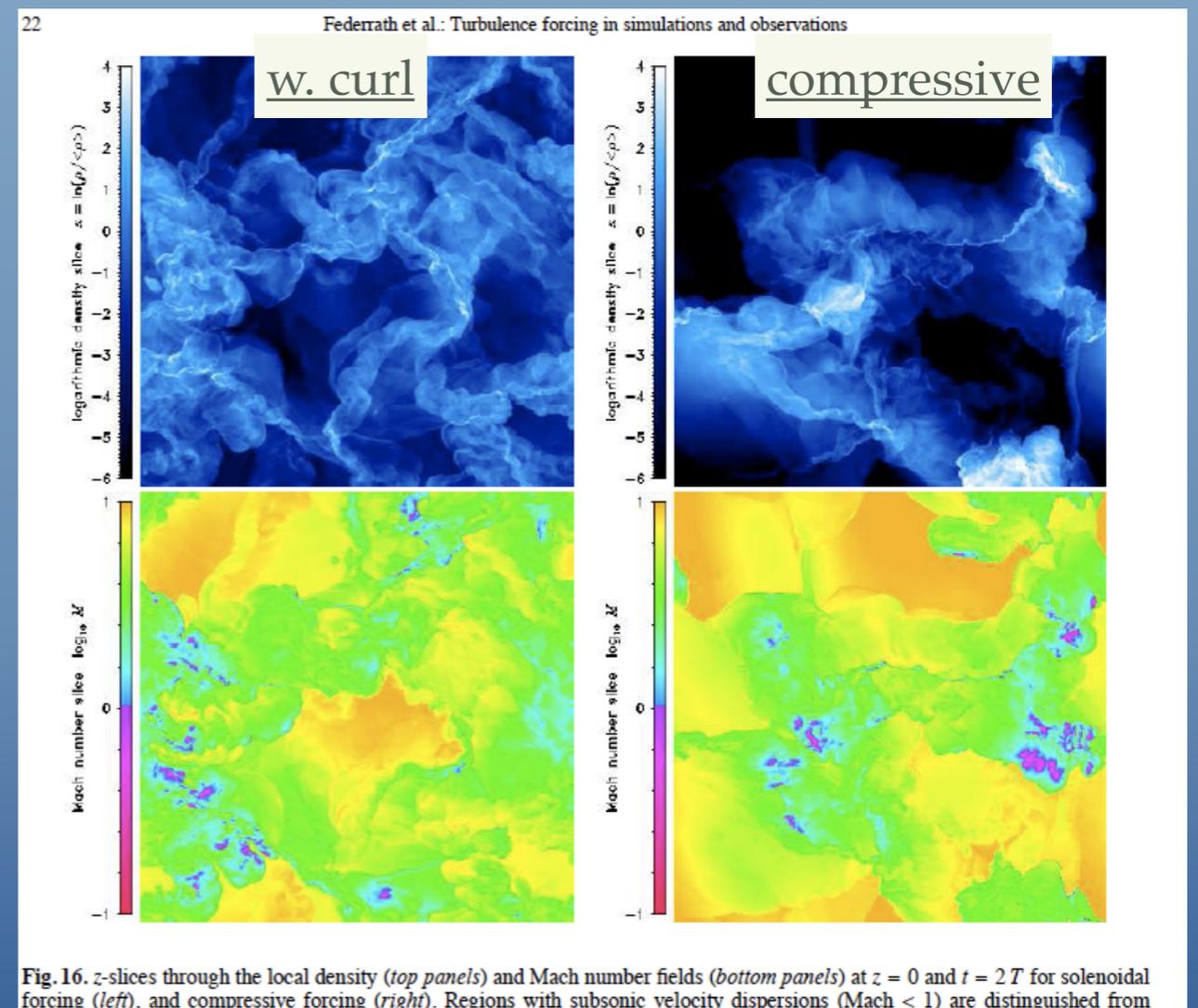
Kinematics in the ρ Ophiuchus region (IRAM 30 m data)
credits : Ph. André et al. 2007, AA

Building up by cooling & accreting: hydrodynamical fragmentation

:: Start from smooth density + randomly-seeded turbulent v-field
(from Bonnell, Bate et al. 2003++, others ..)

- Isothermal gas, FLASHv3
- rotational : $\nabla \cdot \underline{f} = 0$
- compressive : $\nabla \times \underline{f} = 0$
- Stochastic Kolmogorov spectrum
- Shocks, dissipation .. drivers ?

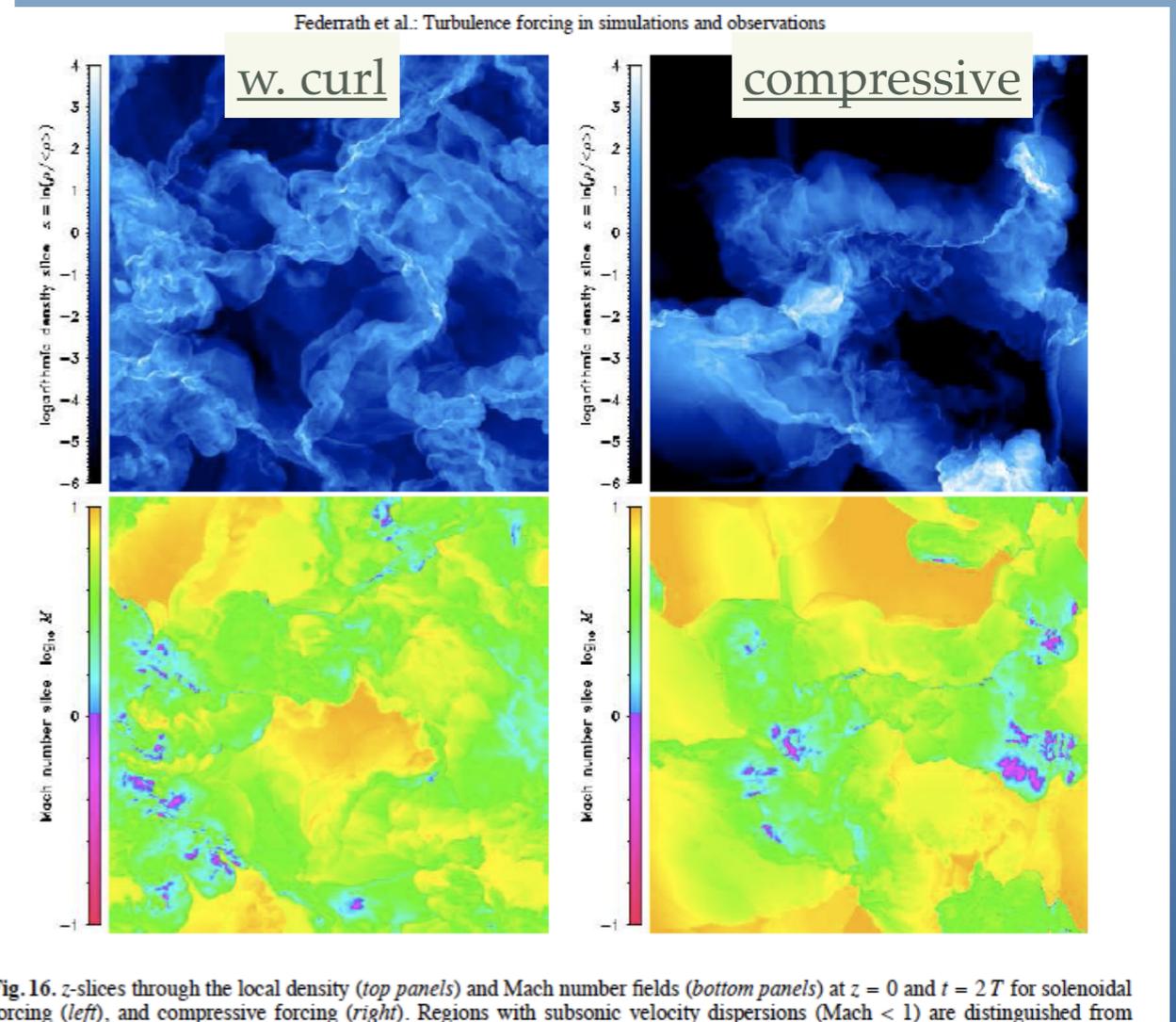
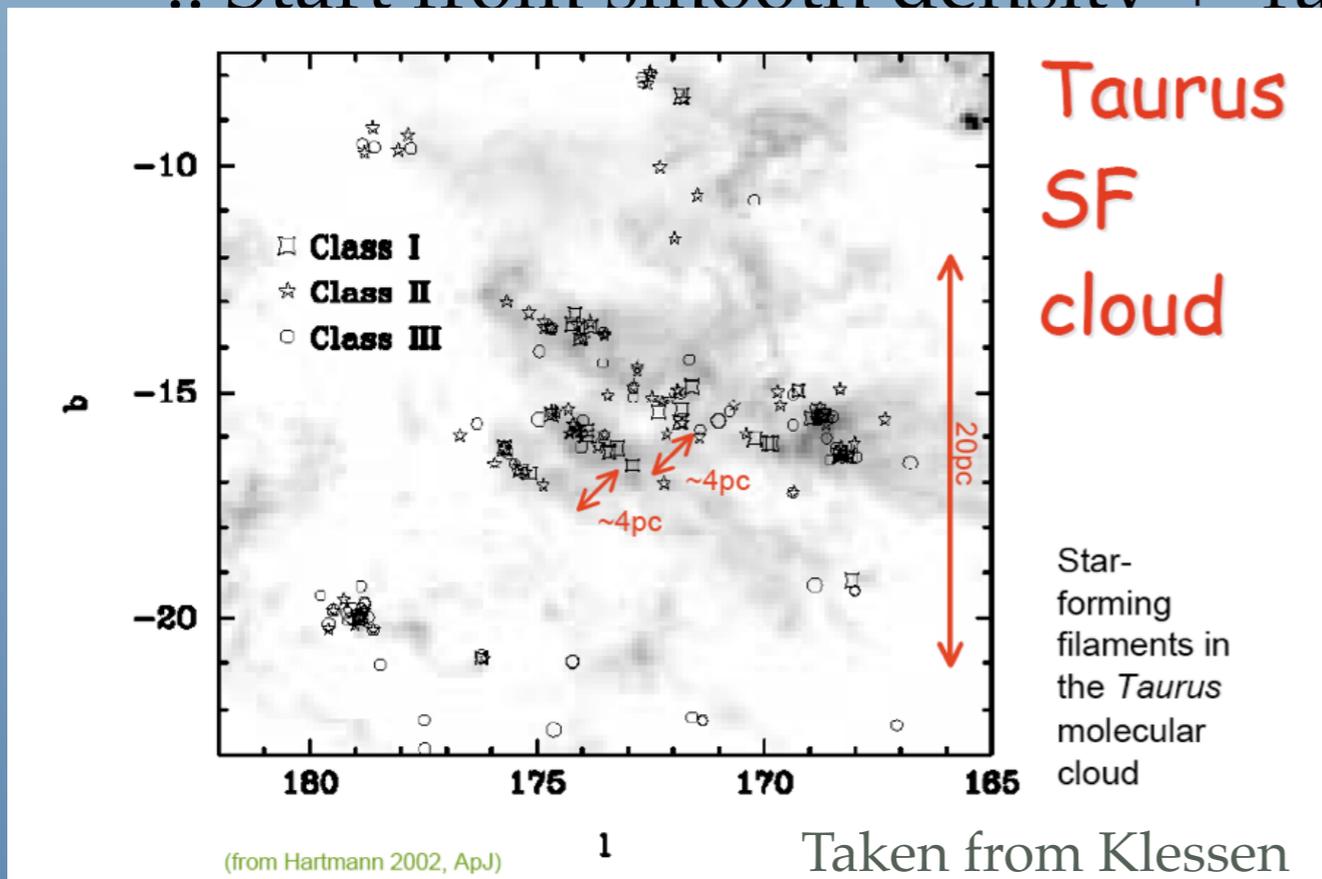
from Federrath et al. 2010



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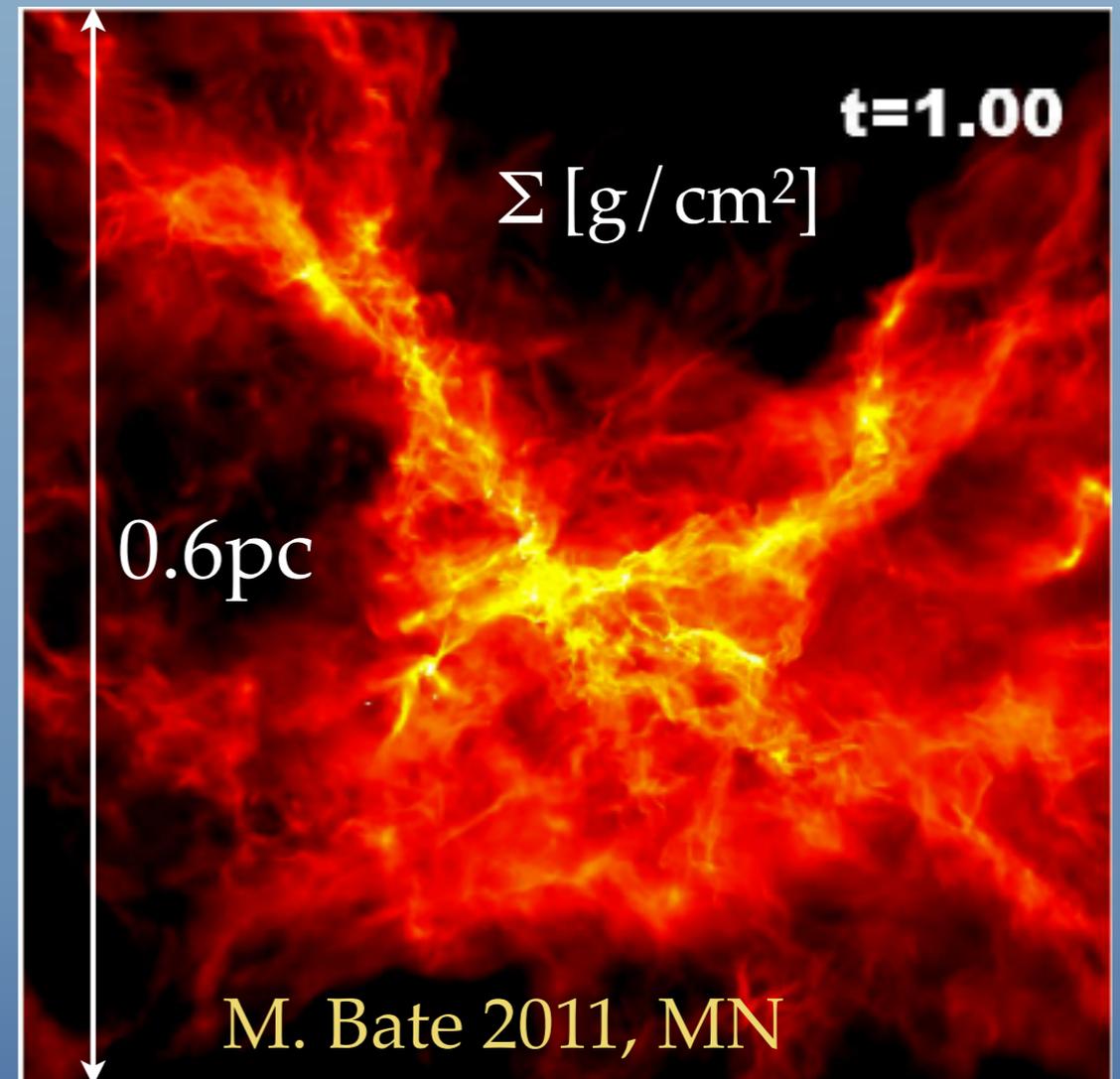


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Fragmentation in star-formation calculations

- ◆ SPH re-simulation of isothermal collapse but *with* opacity
- ◆ Time in units of the free-fall time
 $\sim 2 \times 10^5$ yrs
- ◆ From 250 \triangleright 180 cores formed
($\rho \approx 1.8 \times 10^3 M_{\text{Sun}} / \text{pc}^3$ initially)
- ◆ $M = 500 M_{\text{Sun}}$, $R_0 \approx 1/2 \text{ pc}$ $T \approx 10 \text{ K}$
- ◆ Linear resolution $\sim 0.5 \text{ AU}$



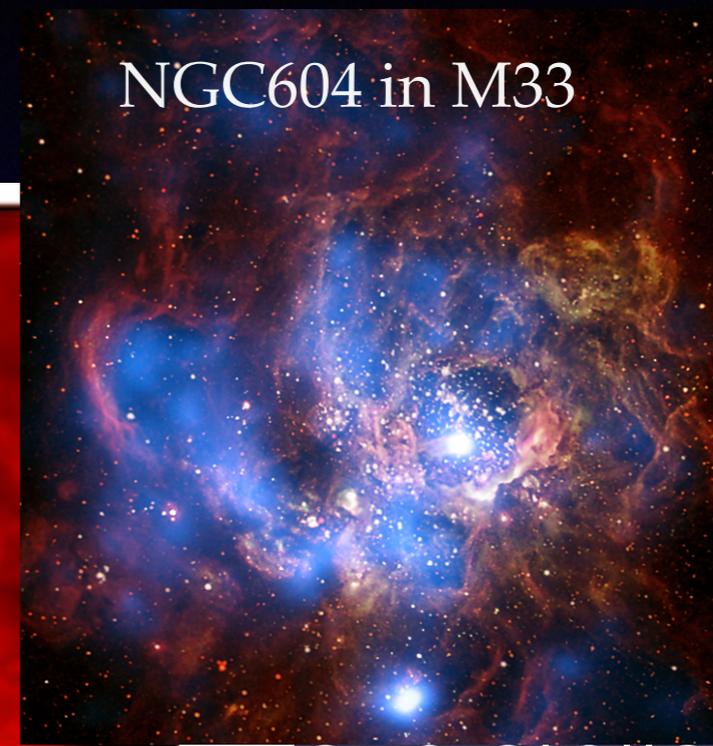
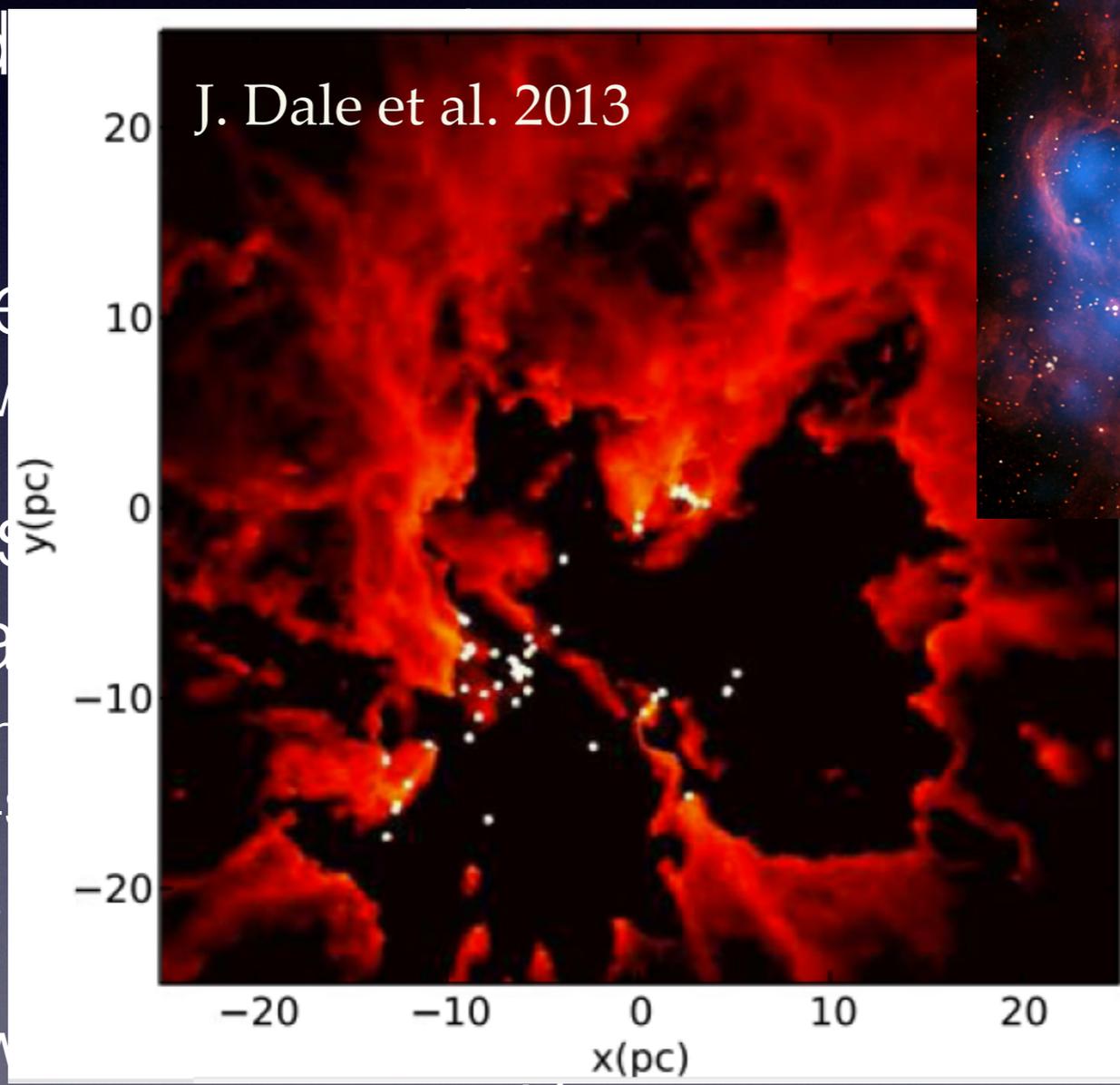
Still ~ 3 orders of magnitude from rich clusters

Transition : embedded \triangleright gas-free. Yes, but how .. ?

- embedded cores / associations m.f. \sim cluster m.f.
-  details of mass-loss unclear, slower than energy argument would suggests (winds, SN, .. *e.g.* J. Dale 10/2015 webcast STScI; S. McMillan, op. recit.) \triangleright boost survival rate
- active star-forming regions with gas have stellar kinematics compatible with *in-situ* star formation (*e.g.* ρ Ophiucus [André et al. 2007] or NGC1333 where $\sigma \sim 0.8$ km/s [Foster et al. 2015, In-Sync survey])
-  *Global* phase-mixing and relaxation on a time-scale well exceeding the star-formation time-scale

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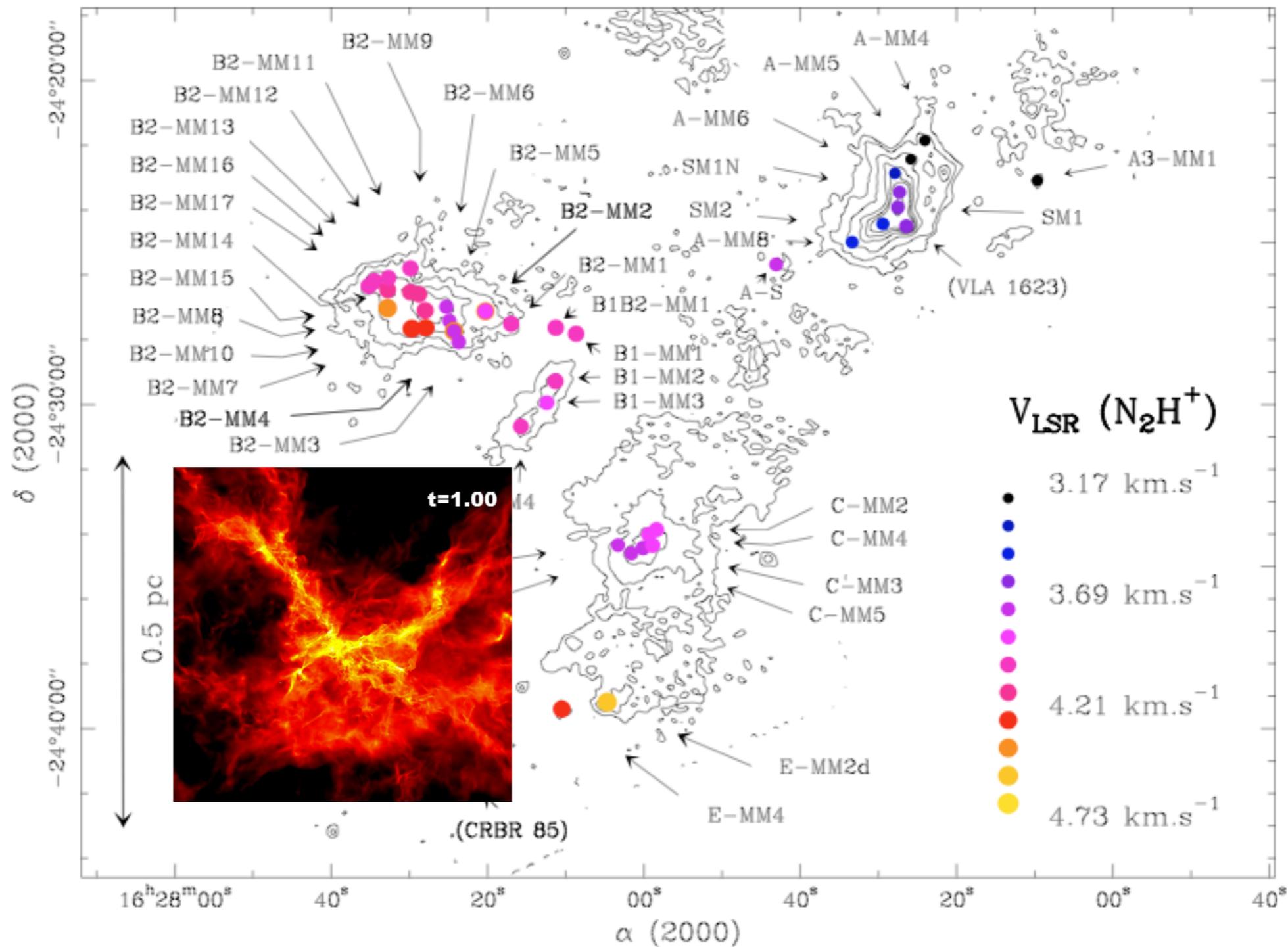
- embedded
- details
- arguments
- active
- kinematics
- *Global*
- scale



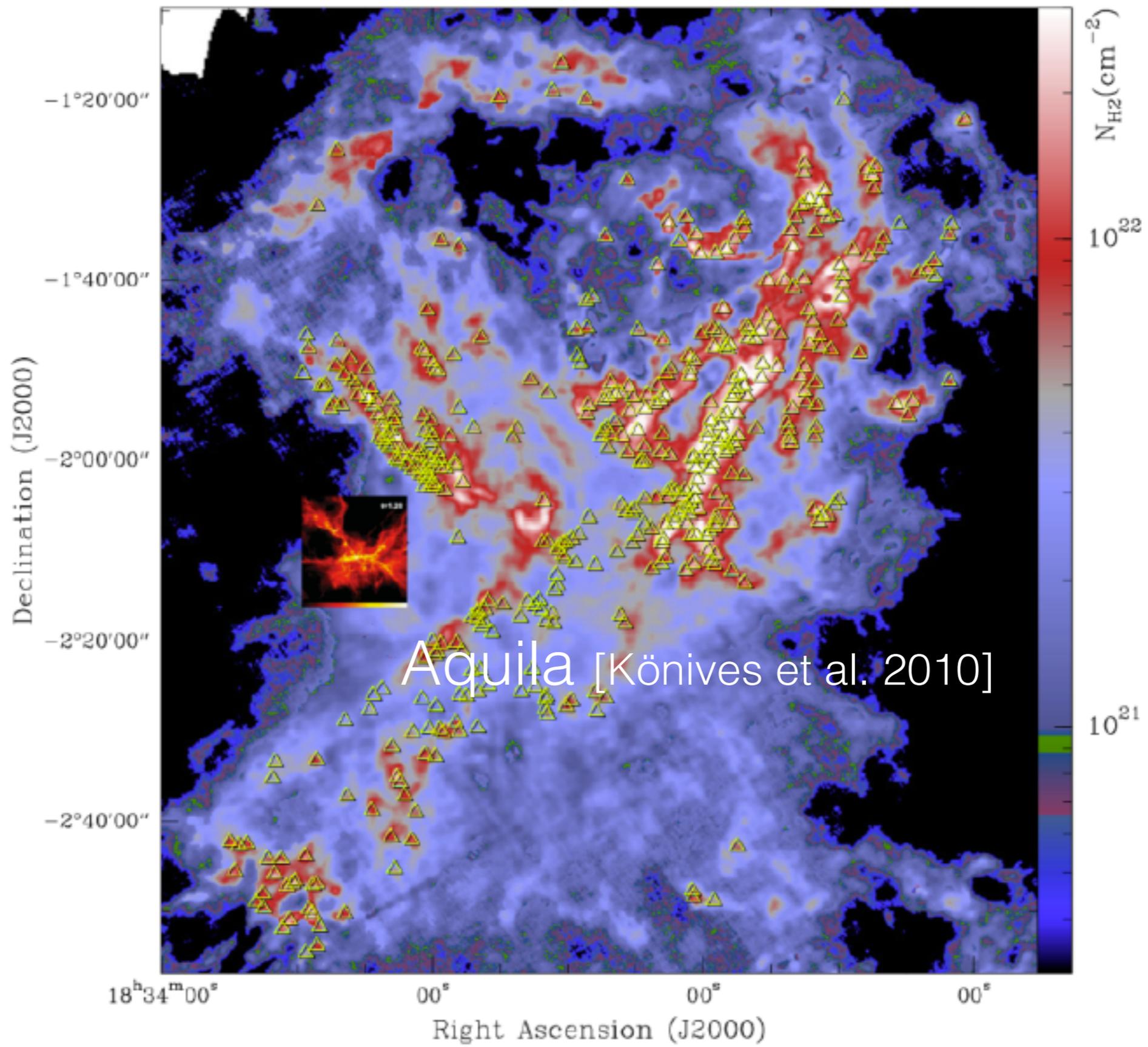
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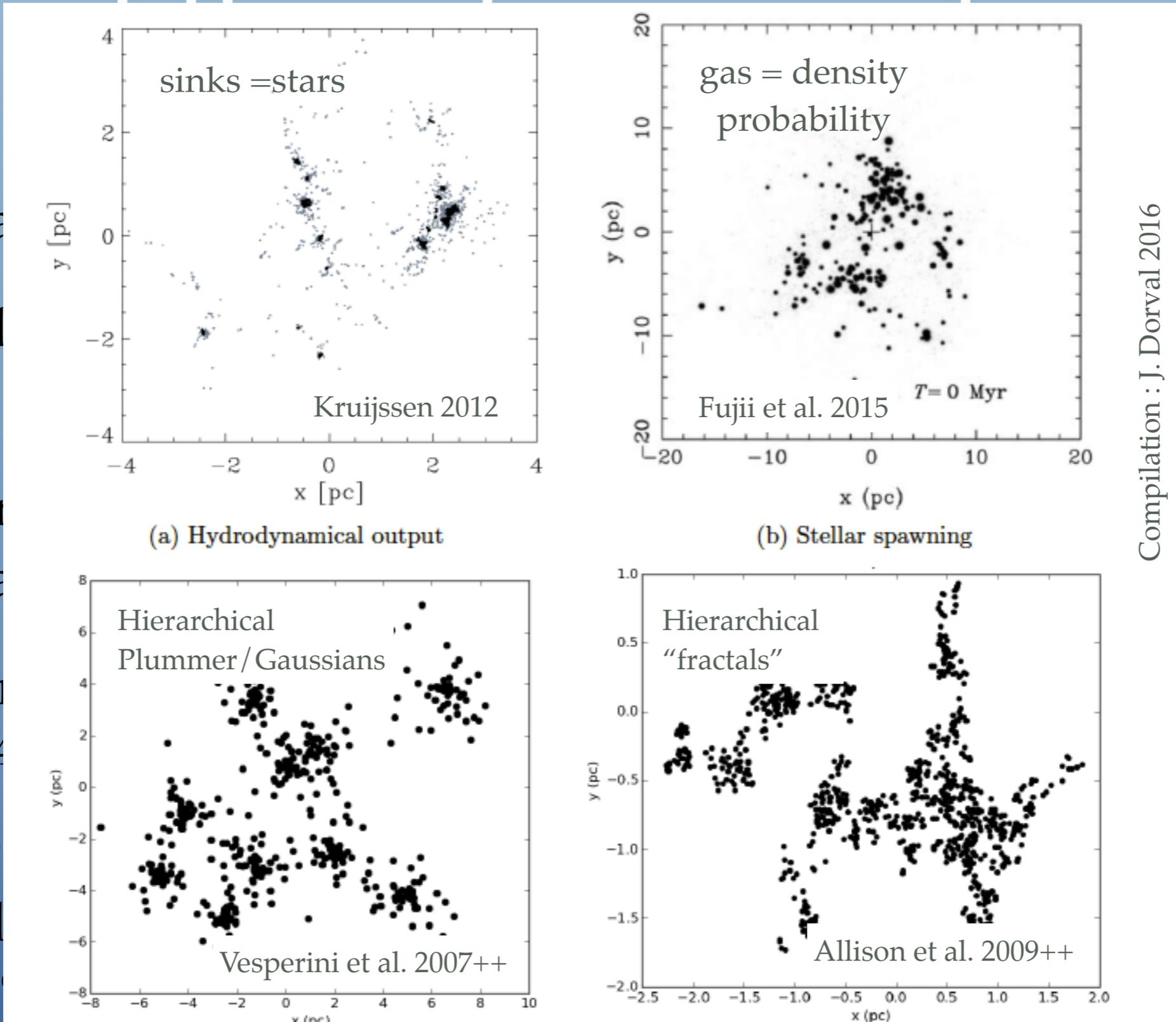


Initial conditions for stellar dynamics: different approaches

- Classic argument: stars are *as cool/cold as gas* is $\sigma^2 \approx k_{\beta}T$
- ■ All mixed up, no mass- or length scale: monolithic collapse, no structure in density or velocity
- Some spatial profile (King, Plummer, ..) with velocities drawn from «equilibrium» d.f. (e.g. Caputo et al. 2014, ..)
- Turbulence imprints young stellar spatial distributions (W43 - Nguyen et al. 2013; G0.253+0.016 / ALMA, Rathborne et al. 2015)
- ■ 'Fractal' distribution : looks like star-forming region, but velocities odd, ad hoc (Goodwin & Withworth 2004, R. Allison et al. 2009++, B. Elmegreen 1997, ..)

Initial conditions for stellar dynamics:

- Classification
- All
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Compilation : J. Dorval 2016

$k_{\beta} T$

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(4, ..)

ns

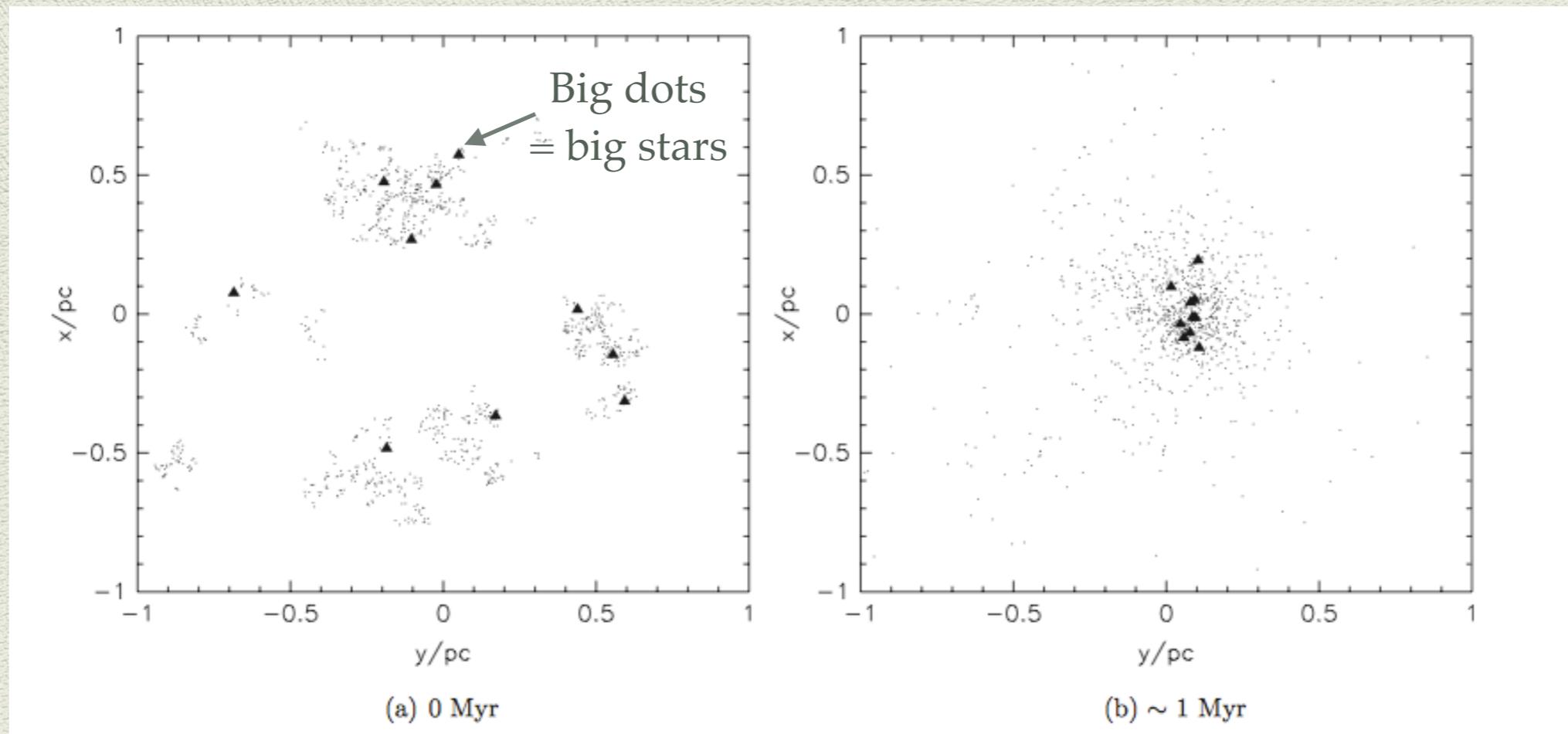
al. 2015)

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son et al.

Initial conditions : fractals

➔ “Fractal” distribution : looks like star-forming regions, but velocities odd, ad hoc (e.g. Allison et al. 2009, 2010)



:: Mass segregation enhanced during relaxation (Vesperini et al 2007, '12, '15)

Segregation in young stellar populations : OB star in Carina

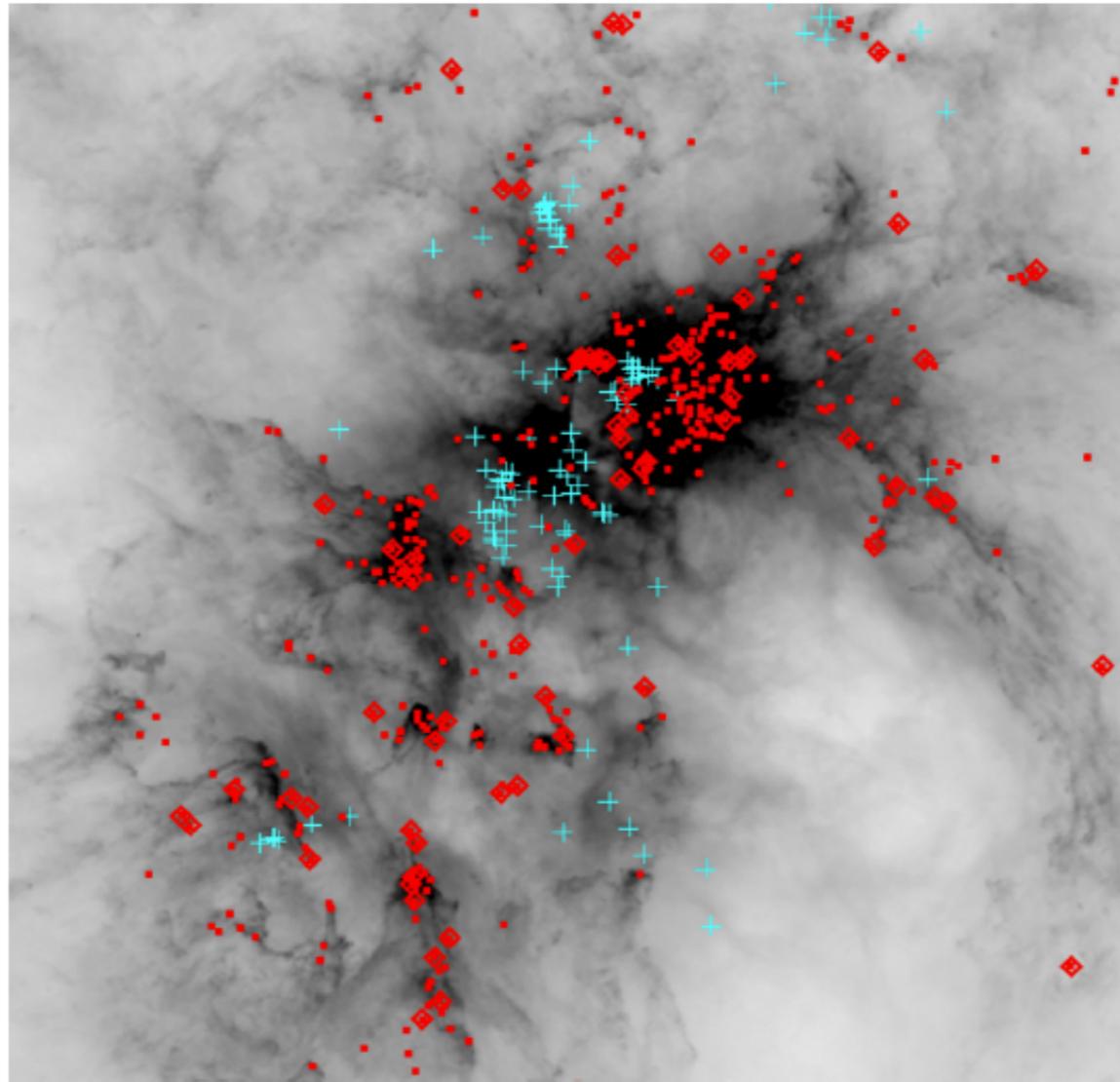


Figure 1.8: Herschel IR 70m observations of the Carina Nebula, with YSOs as red points and diamonds. Cyan crosses show OB stars. Both the gas and prestellar objects follow a substructured distribution. The figure was extracted from [Gaczkowski et al. \(2013\)](#).

Initial conditions: it's bottom up++

Fragmentation modes + collisional evolution

- ❖ Cooling leads to drop in Jean length and the growth of fragmentation modes
- ❖ Cooling by gravity = two-body diffusion of E_k or expansion of entire system (▷ analogy only, not thermal v ; ok with a hard wall [gas pressure])

❖ $TdS = dU + P dV = 0 \quad \therefore dU \downarrow \text{ if } dV \uparrow$

:: Mass segregation develops *during* the fragmentation process



collisional integrator: nb6/++, phiGPU: narrow mass range ok

:: Seek out a *fragmented* configuration with consistent v -field

:: Adiabatic cooling time = star formation time-scale (constraint)

Study the fragmentation of self-gravitating fluids

- Cold fluid perturbed by density fluctuations : linear analysis
- Work on a spherical mesh (boundaries) but with randomly seeded perturbations (in density)

- Write Lagrangian operators

$$\frac{d^2}{dt^2} r' = -\nabla_{r'} (\Phi + \delta\Phi)$$

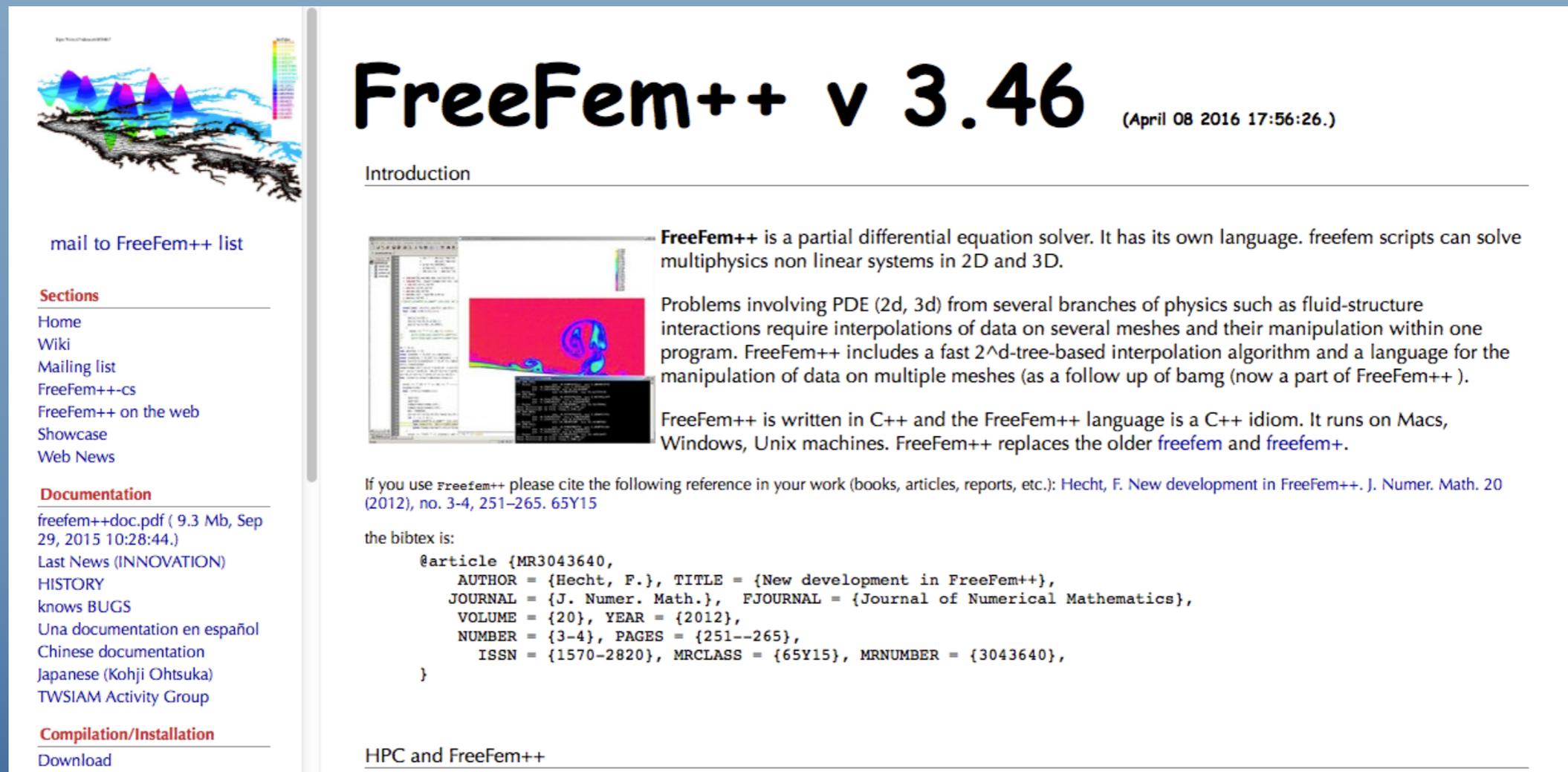
- Integrate .. but stay coherent

$$\nabla_{r'} = \nabla_r + \xi \cdot \nabla_r (\nabla)$$
$$r' = r + \xi$$

Results begin to “look like” star forming regions but something is missing : time + resolution (\triangleright stellar cores)

Fragmentation of self-gravitating fluids

■ <http://www.freefem.org>



FreeFem++ v 3.46 (April 08 2016 17:56:26.)

Introduction

FreeFem++ is a partial differential equation solver. It has its own language. freefem scripts can solve multiphysics non linear systems in 2D and 3D.

Problems involving PDE (2d, 3d) from several branches of physics such as fluid-structure interactions require interpolations of data on several meshes and their manipulation within one program. FreeFem++ includes a fast 2^d-tree-based interpolation algorithm and a language for the manipulation of data on multiple meshes (as a follow up of bamg (now a part of FreeFem++)).

FreeFem++ is written in C++ and the FreeFem++ language is a C++ idiom. It runs on Macs, Windows, Unix machines. FreeFem++ replaces the older *freefem* and *freefem+*.

If you use `FreeFem++` please cite the following reference in your work (books, articles, reports, etc.): Hecht, F. New development in FreeFem++. J. Numer. Math. 20 (2012), no. 3-4, 251–265. 65Y15

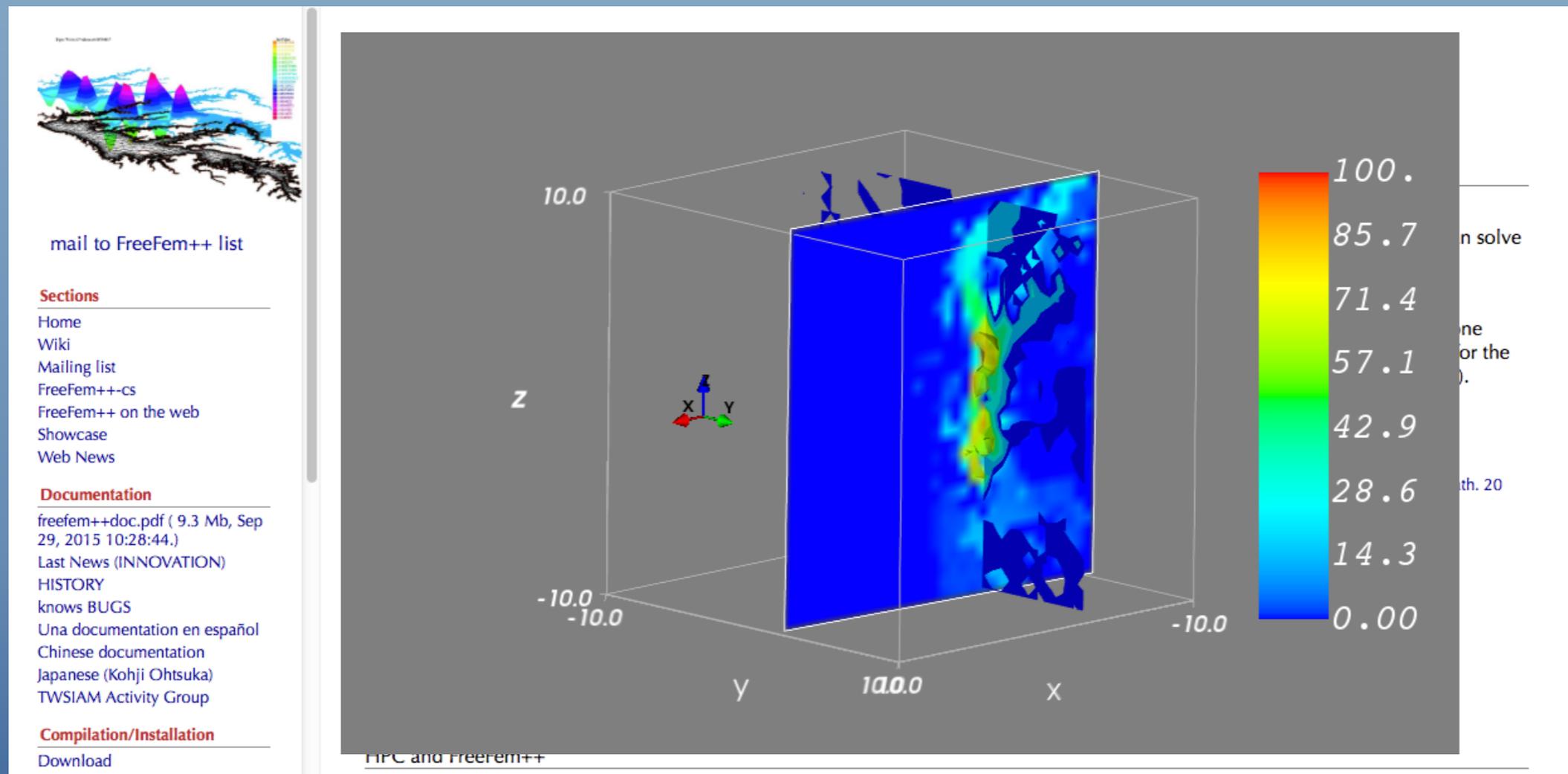
the bibtex is:

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  AUTHOR = {Hecht, F.}, TITLE = {New development in FreeFem++},
  JOURNAL = {J. Numer. Math.}, FJOURNAL = {Journal of Numerical Mathematics},
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  NUMBER = {3-4}, PAGES = {251--265},
  ISSN = {1570-2820}, MRCLASS = {65Y15}, MRNUMBER = {3043640},
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HPC and FreeFem++

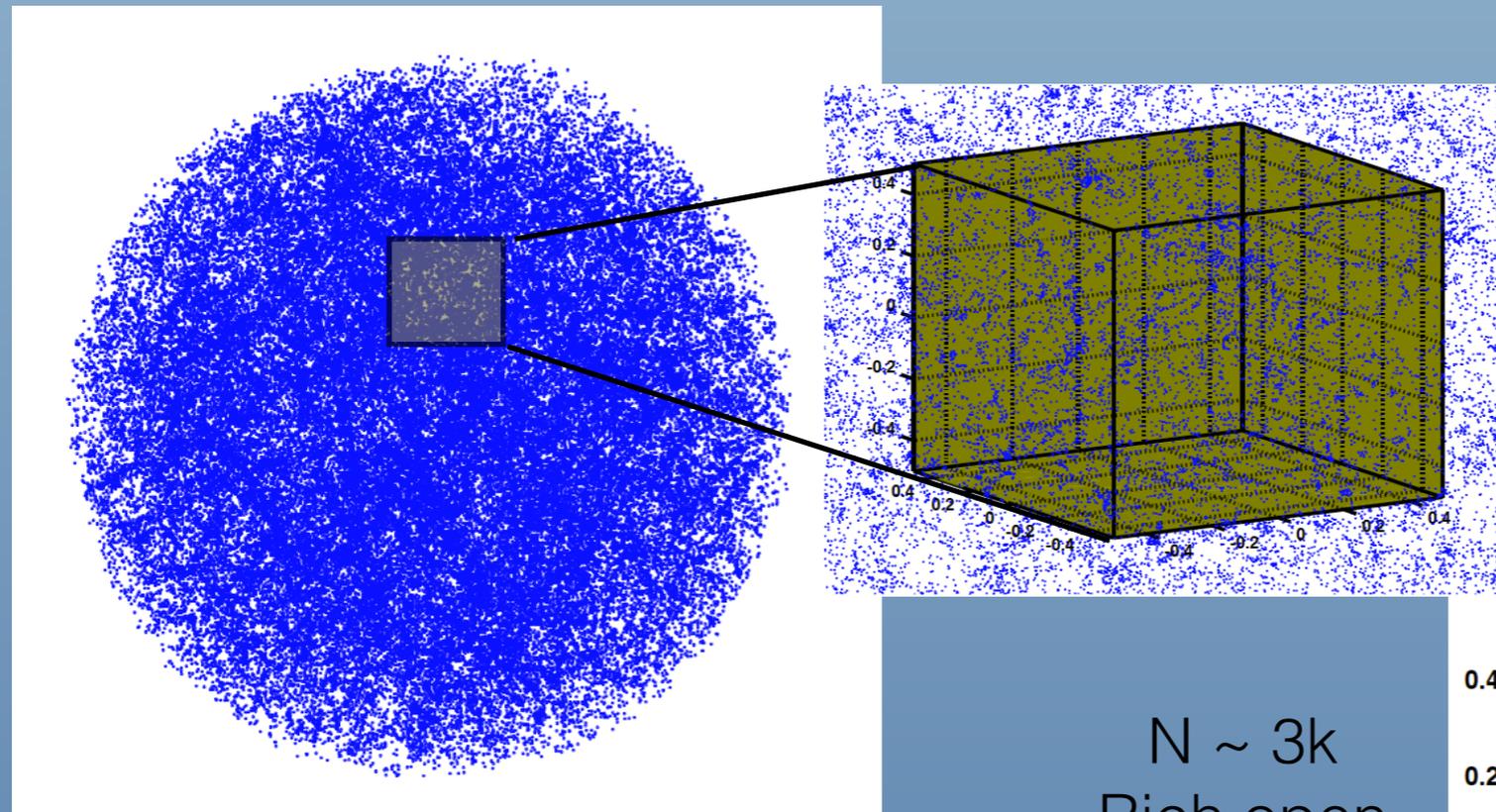
Fragmentation of self-gravitating fluids

■ <http://www.freefem.org>



Procedure - avoid boundaries

Dorval et al. 2016 MNRAS, 2017

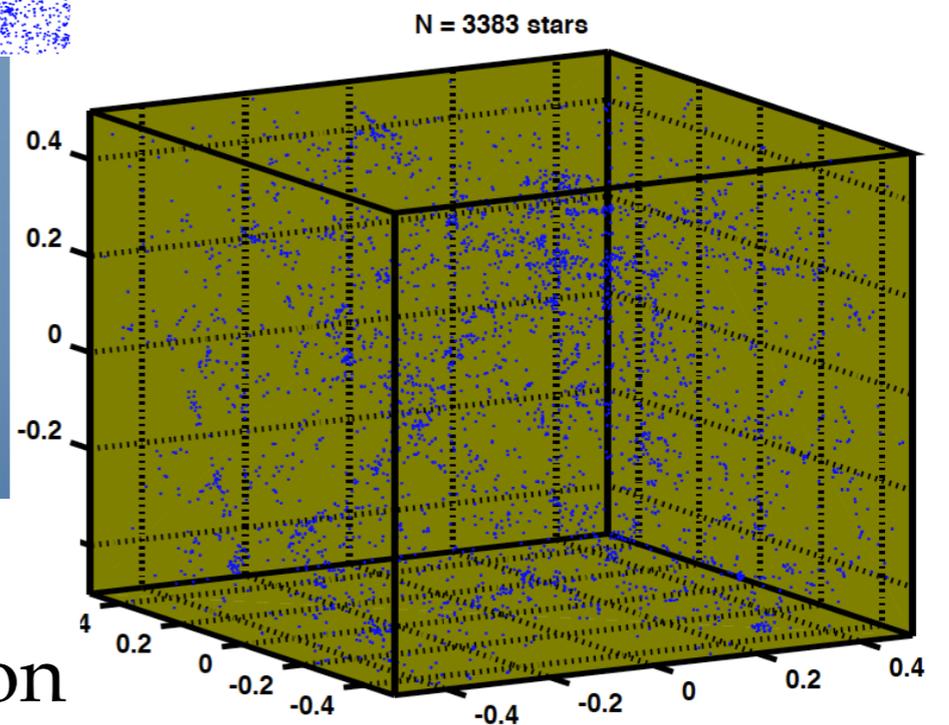


$N \sim 100k$ stars

$N \sim 3k$
Rich open
cluster

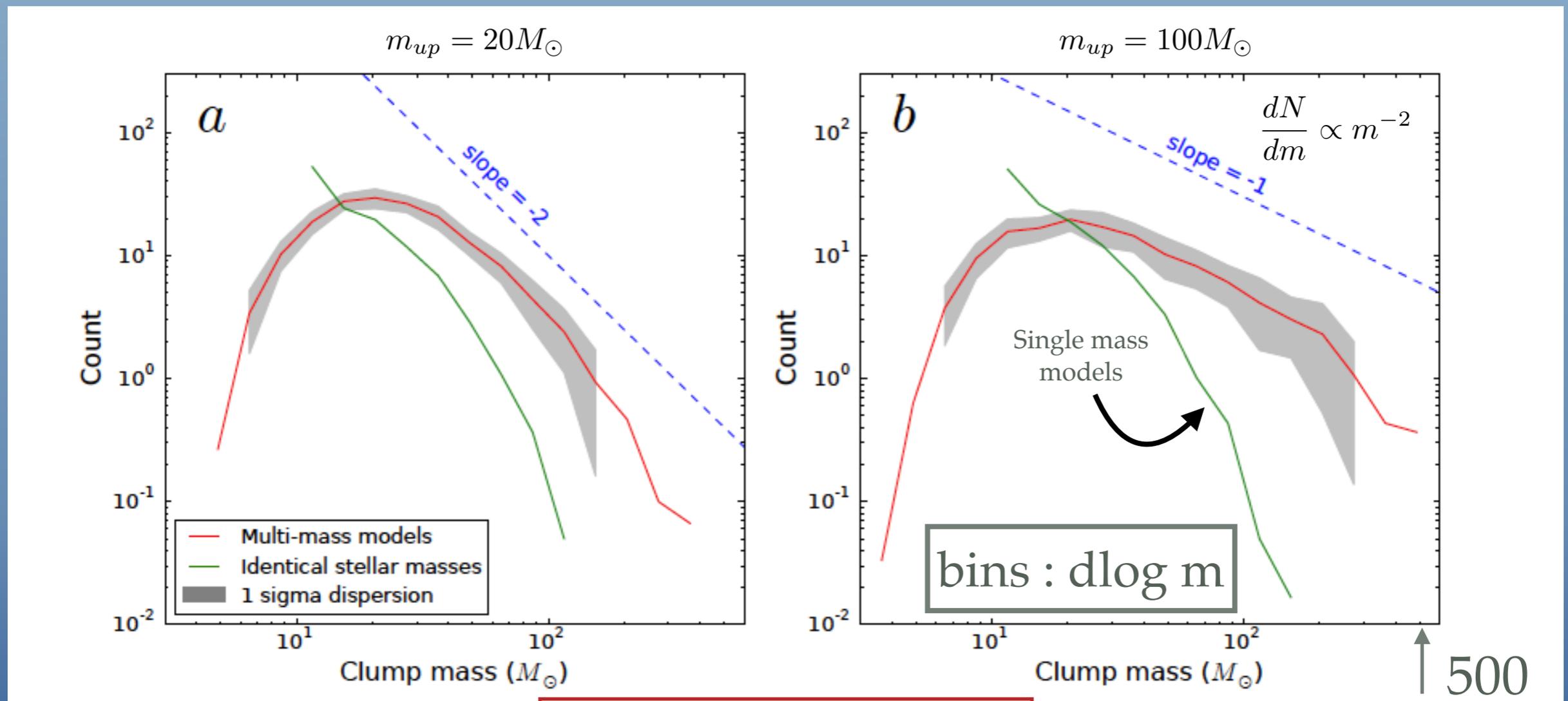
Extract
subset of
stars
clumps: MST technique

- Draw stars from IMF (Salpeter)
- Form binaries with primary-★ correlation



Stellar clumps: mass function, and stellar m.f.

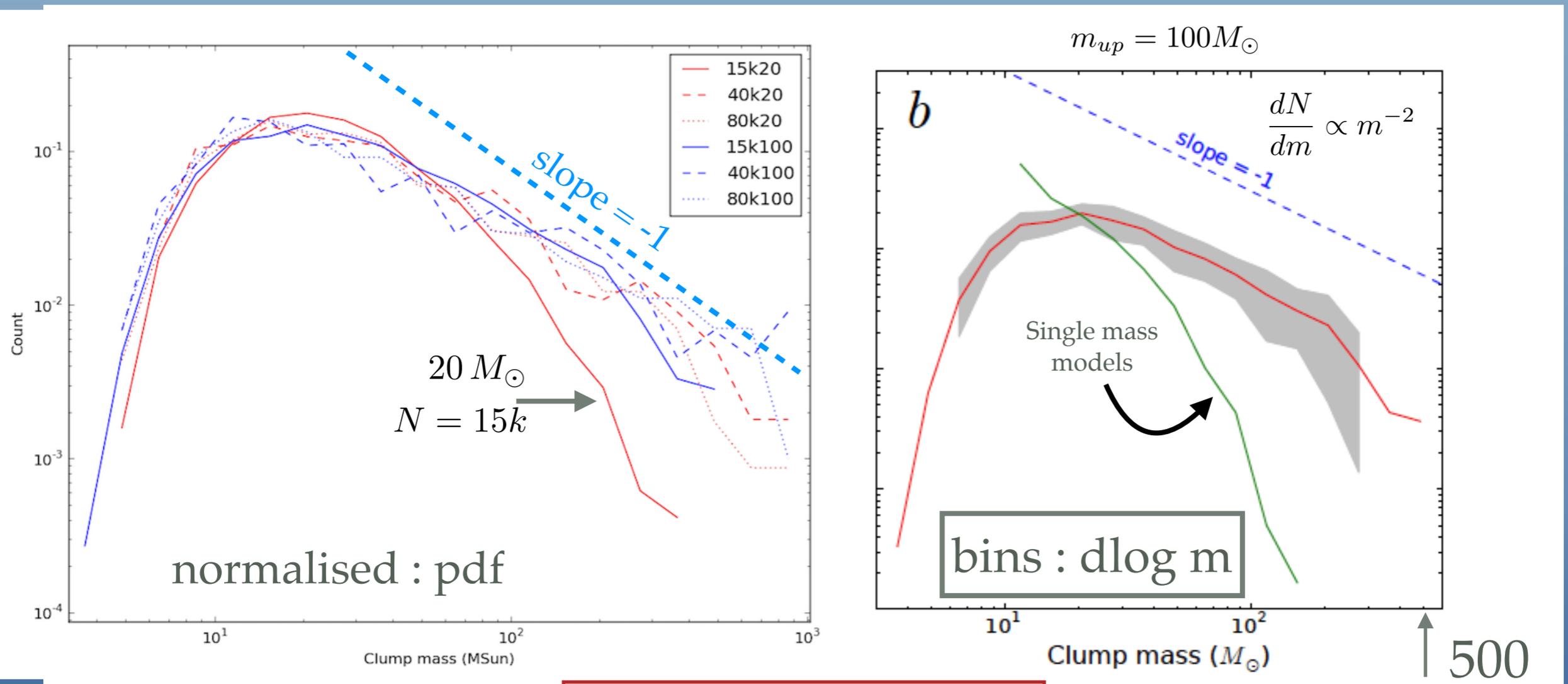
Equal-mass models vs Salpeter IMF (two upper truncation values)



Runs with $N = 15k$

Stellar clumps: mass function, and stellar m.f.

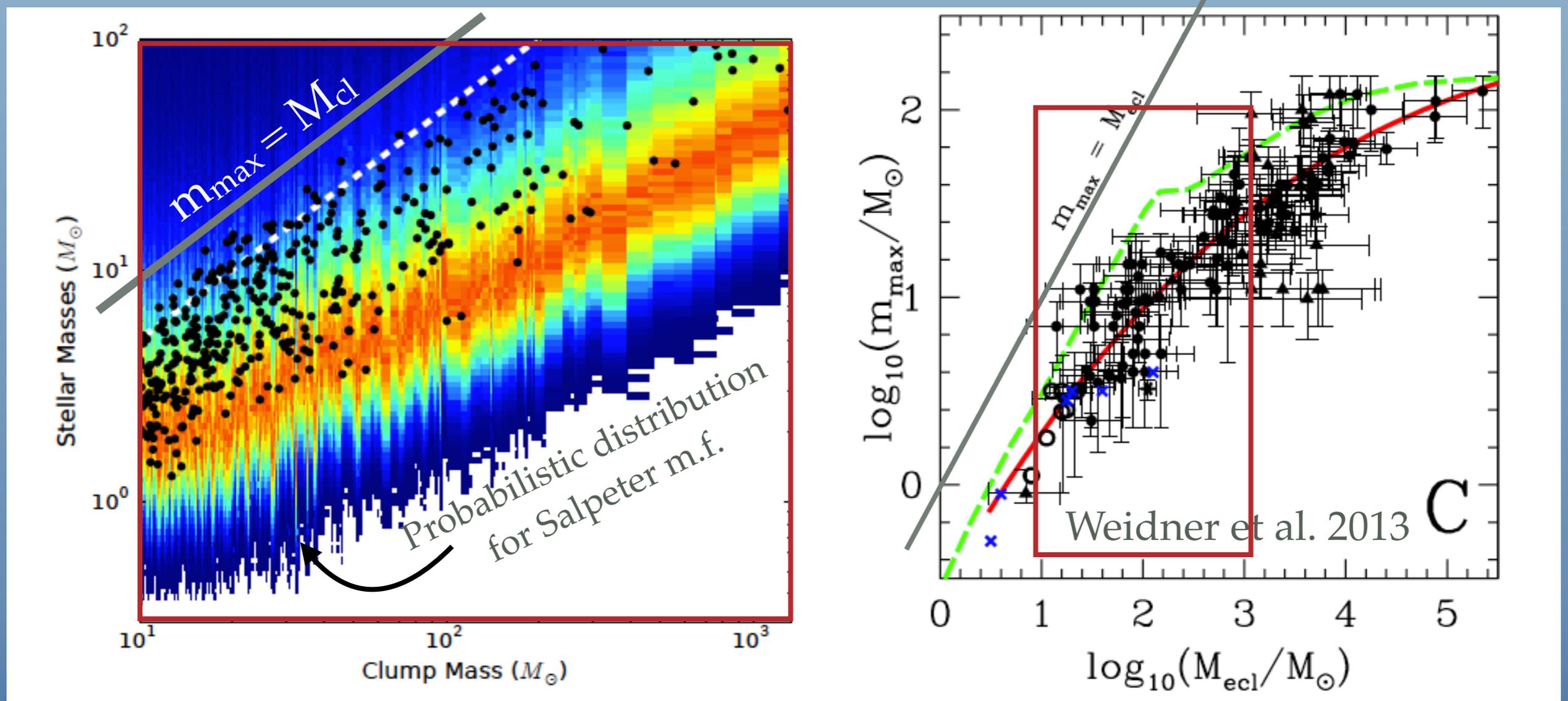
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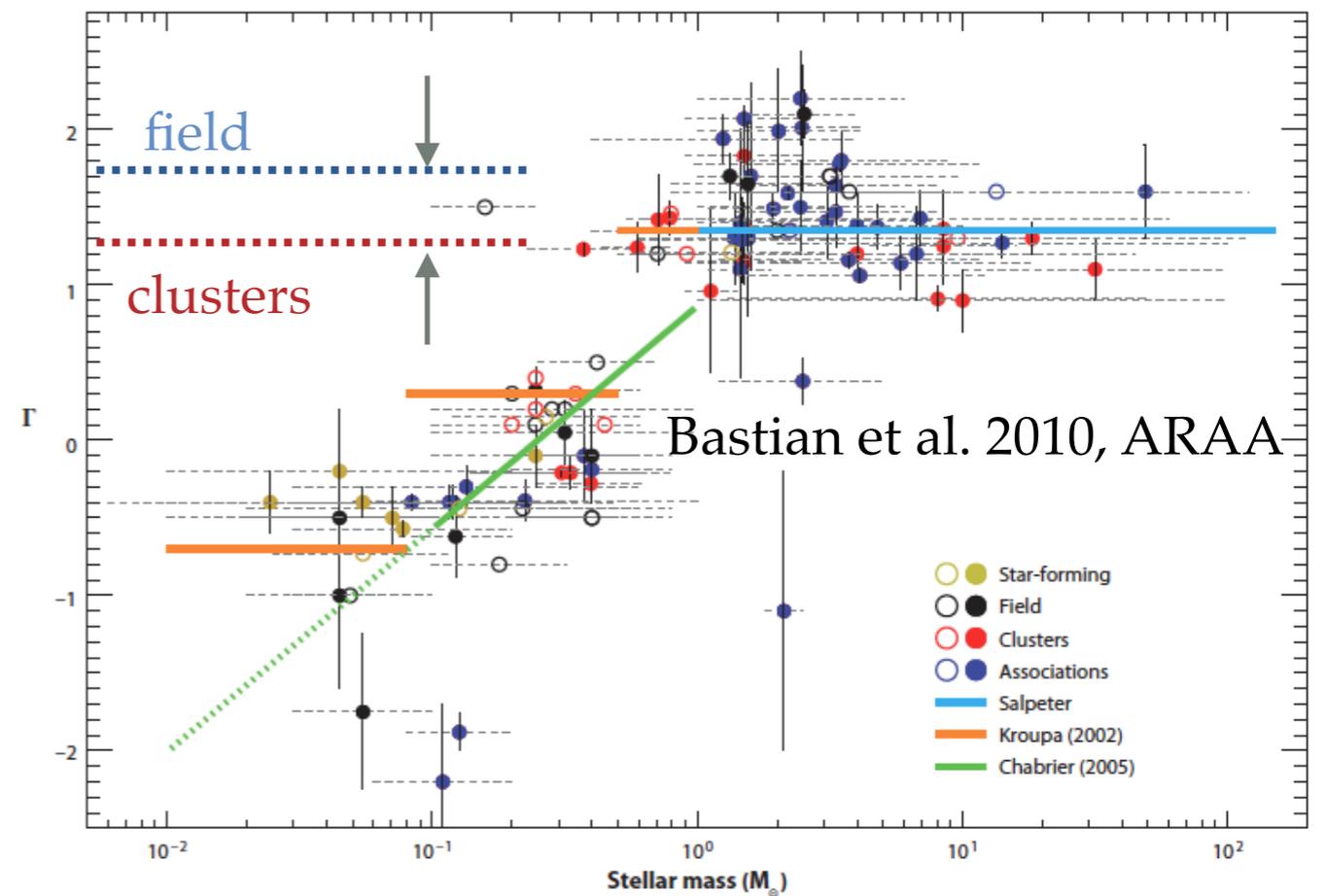
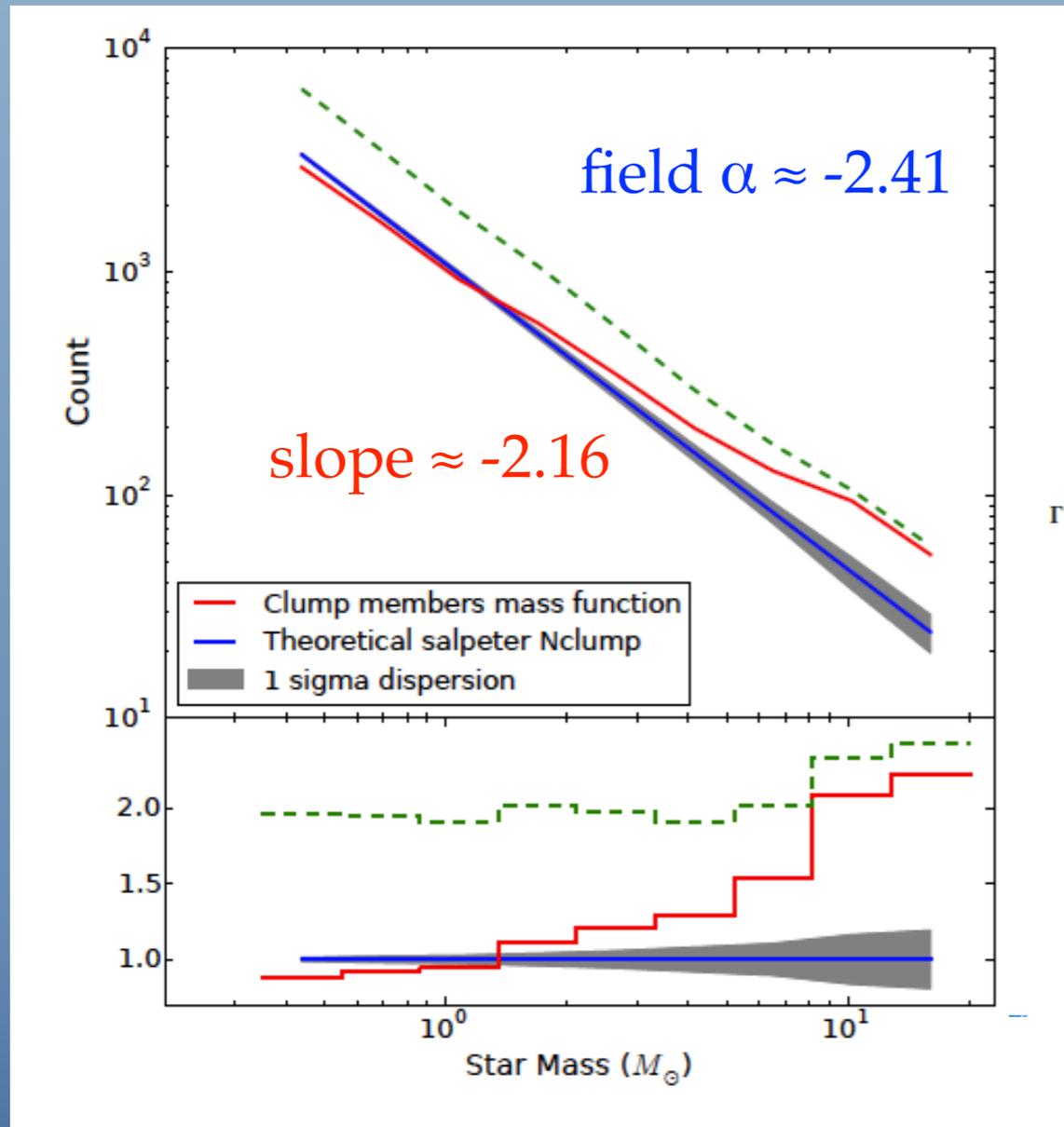
Stellar clumps:

correlation with $\max\{m_{\star}\}$



:: white dash: prediction from «radius of influence» of most massive star in clump

Stellar clumps: 50% of all stars top-heavy, segregated ..



:: blue / grey : Salpeter (ensemble averaging)

Stellar clumps: 50% of all stars top-heavy, segregated ..

Maschberger et al.
2010

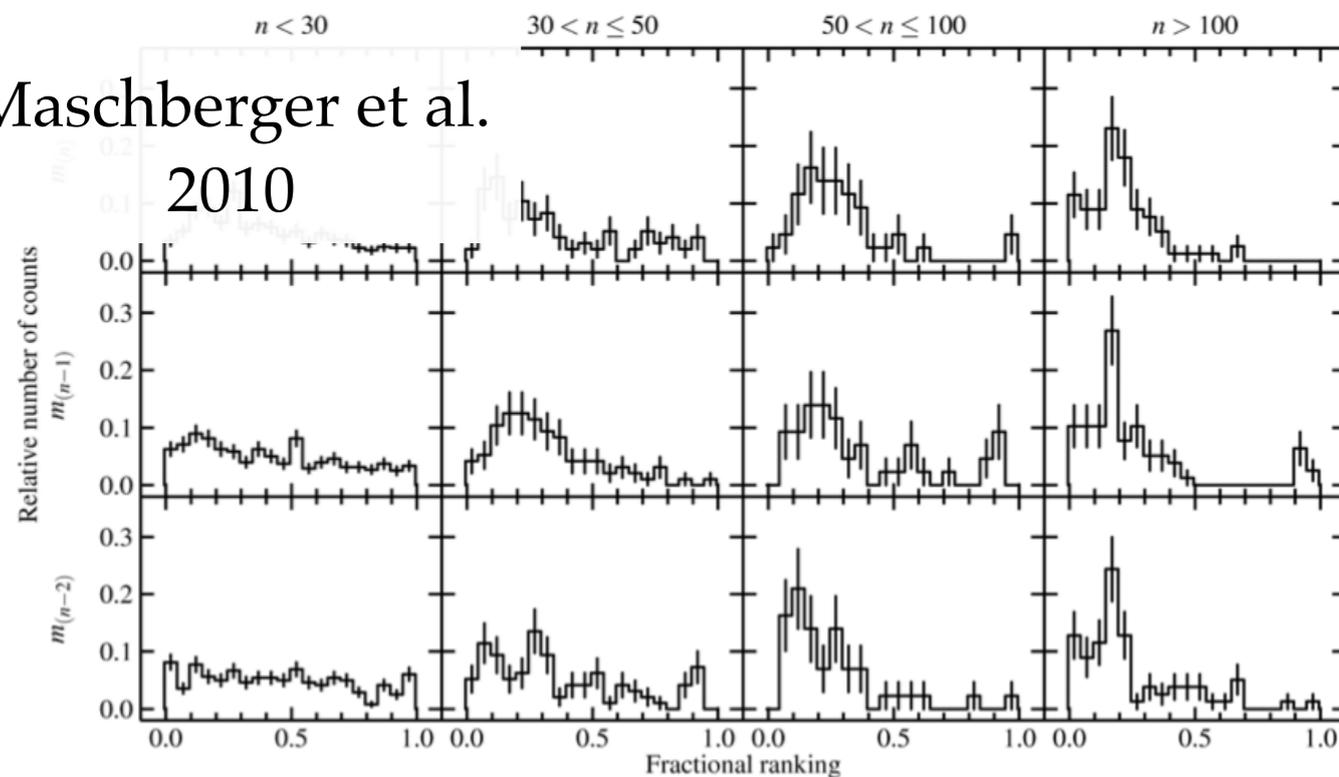


Figure 13. Histogram of the fractional radial ranking of the most massive (top), second most massive (middle) and third most massive (bottom) sink in its associated subcluster, split up by the number of sinks in the subcluster. The composite population of the $10^4 M_{\odot}$ calculation is used to make the histogram. In the absence of mass segregation, the histogram would be flat: the peak at small values shows that the massive sinks are preferentially found near the centre. The second peak with a ranking of ≈ 1 , especially for the second and third most massive sink, is due to mergers, where two centres are still present.

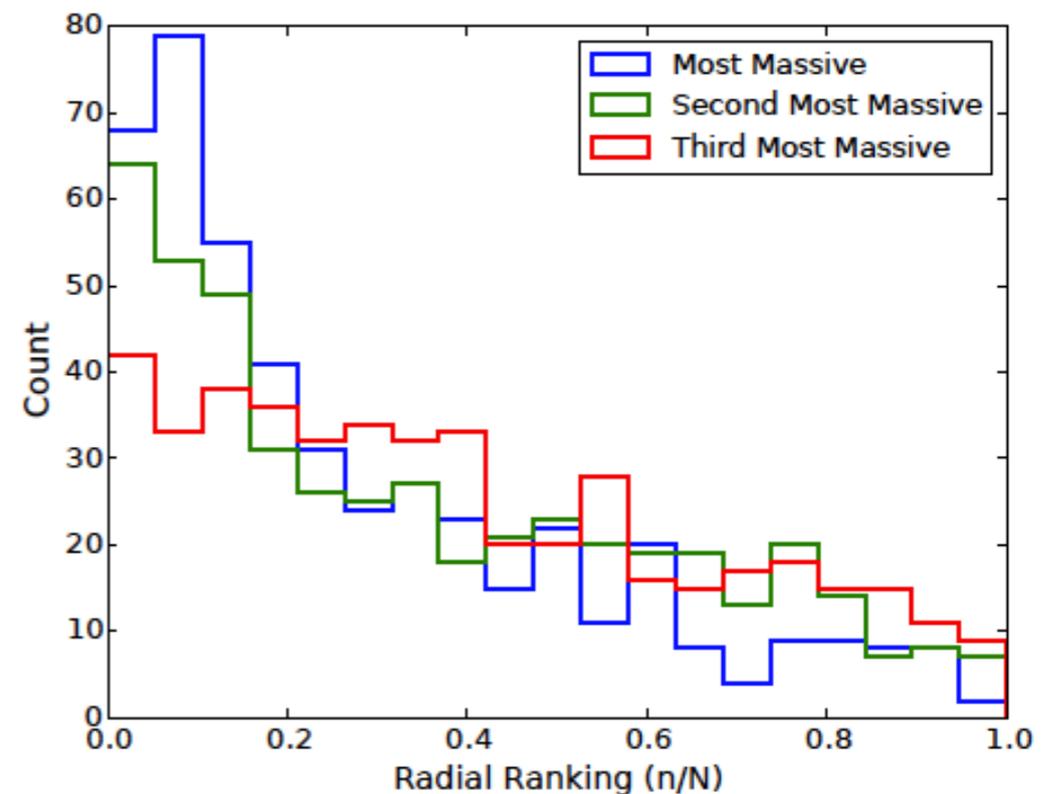


Figure 10. Radial ranking of first, second and third most massive star in each clump for a model with $N = 40\,000$ stars (R40h100).

Ranking diagnostics of Maschberger et al. (2010) for hydro simulation

cf. Vesperini, McMillan 2007, -12, -15

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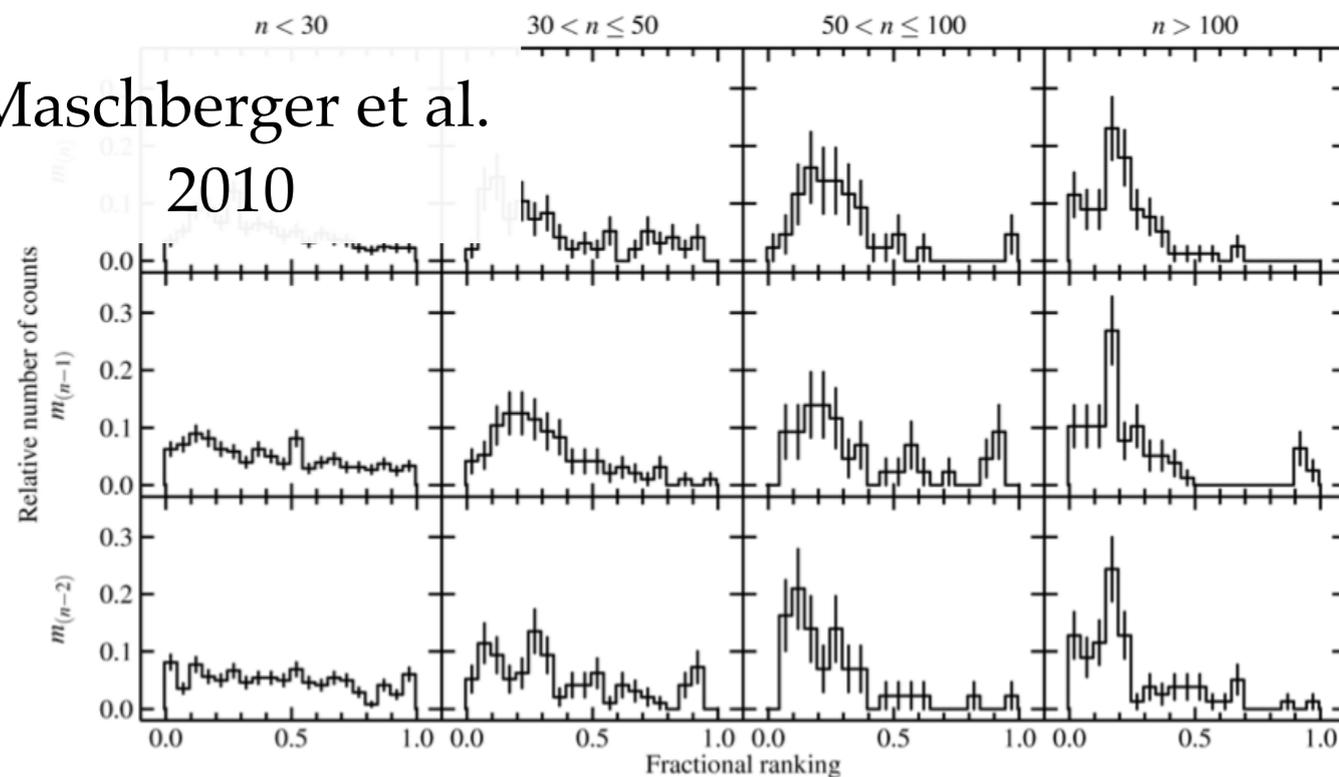


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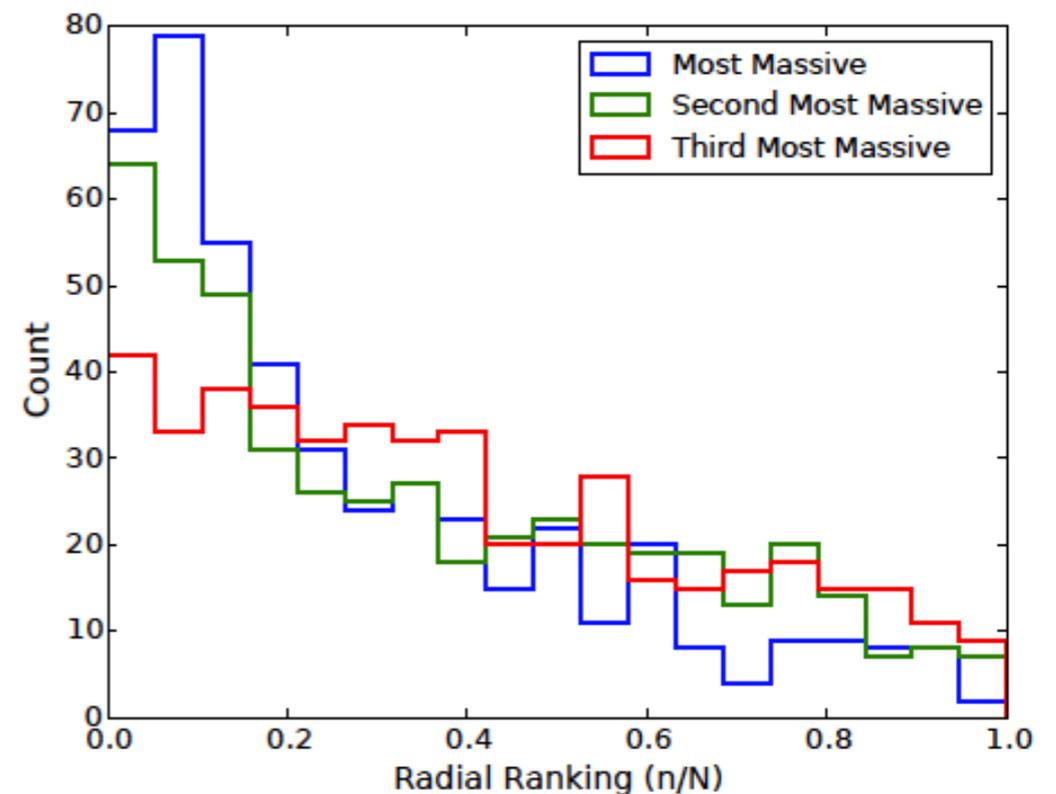


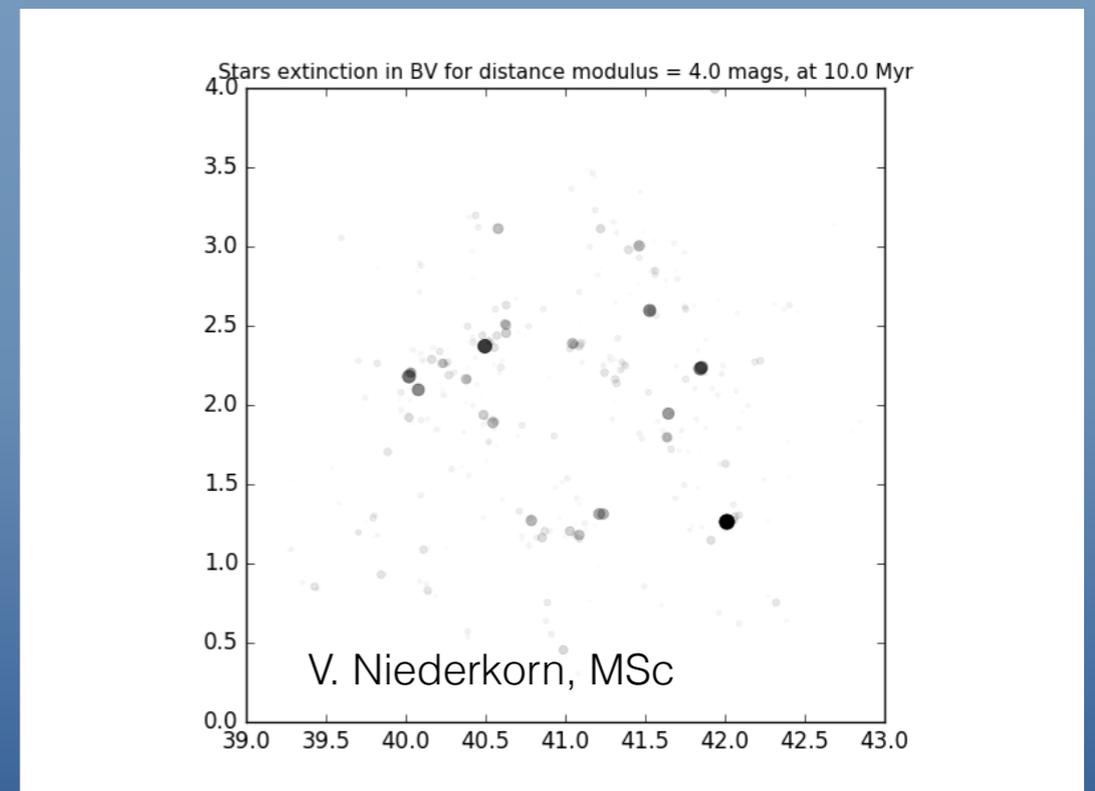
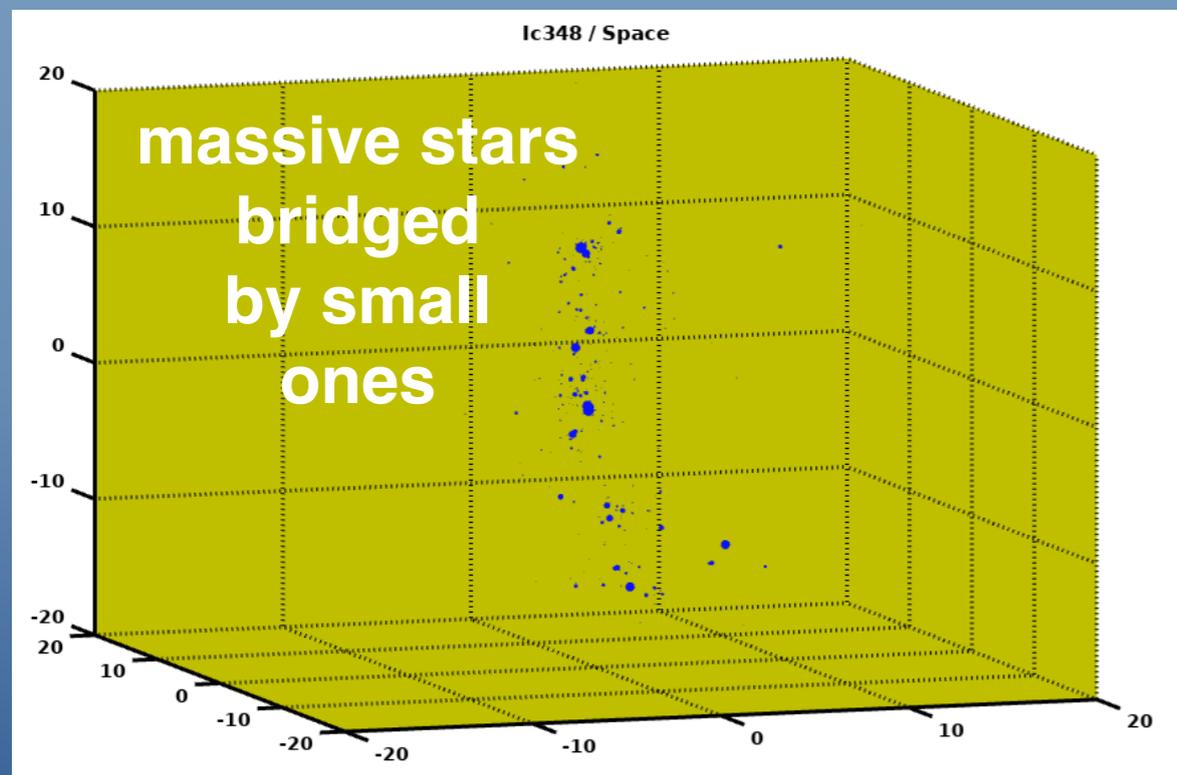
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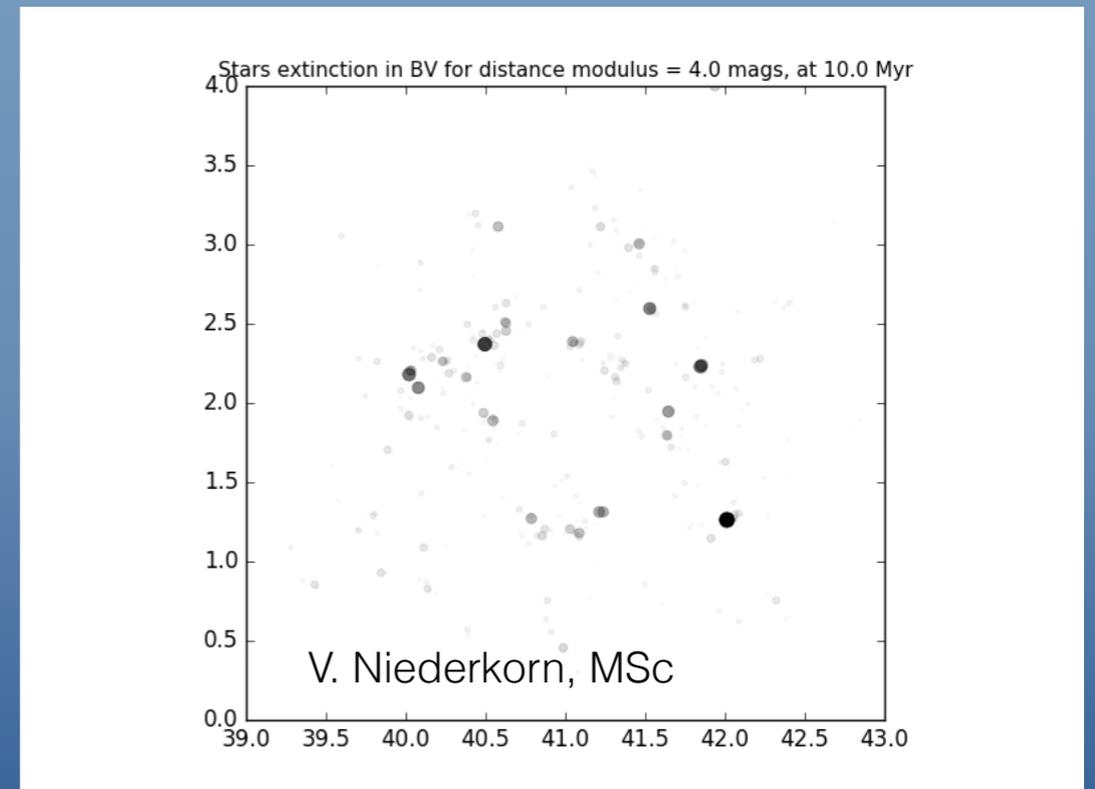
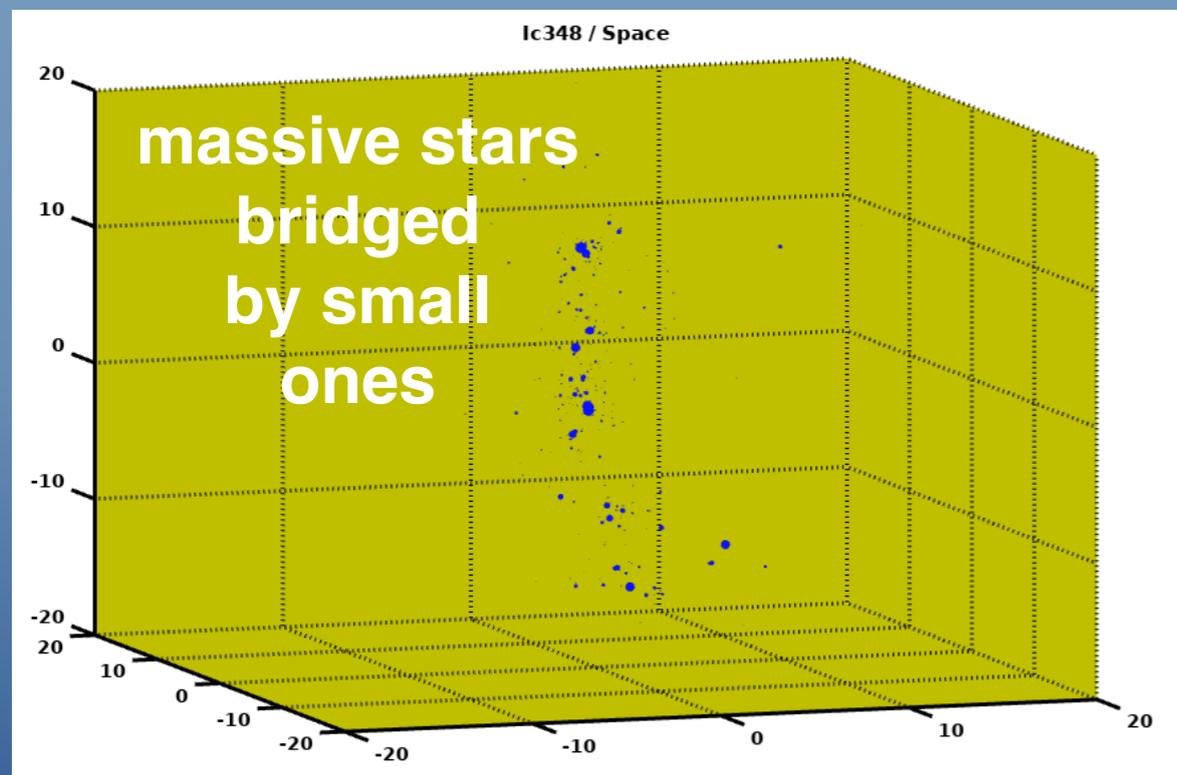
Exploring morphology using the Minimum Spanning Tree approach

- ◆ Morphology : apparent vs real .. selection, extinction
- ◆ Use the Pan-Starrs 1 extinction map (Green et al. 2015, ..)
- ◆ Set up a clump with $N \sim 400$ stars (e.g. Ic348)
- ◆ Photometry, bolometric corrections: set the object at different DM



Exploring morphology using the Minimum Spanning Tree approach

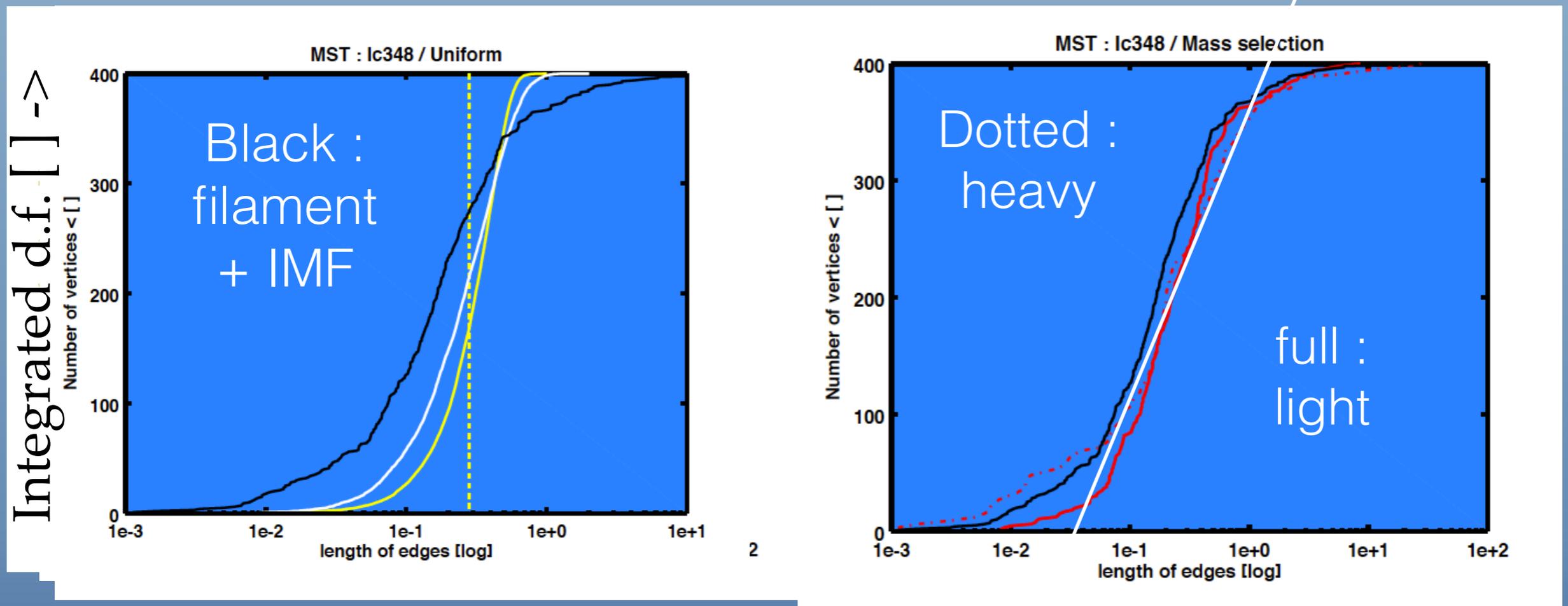
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Exploring morphology using the Minimum Spanning Tree, all member stars

Different projection angles

Selection by mass / renormalized



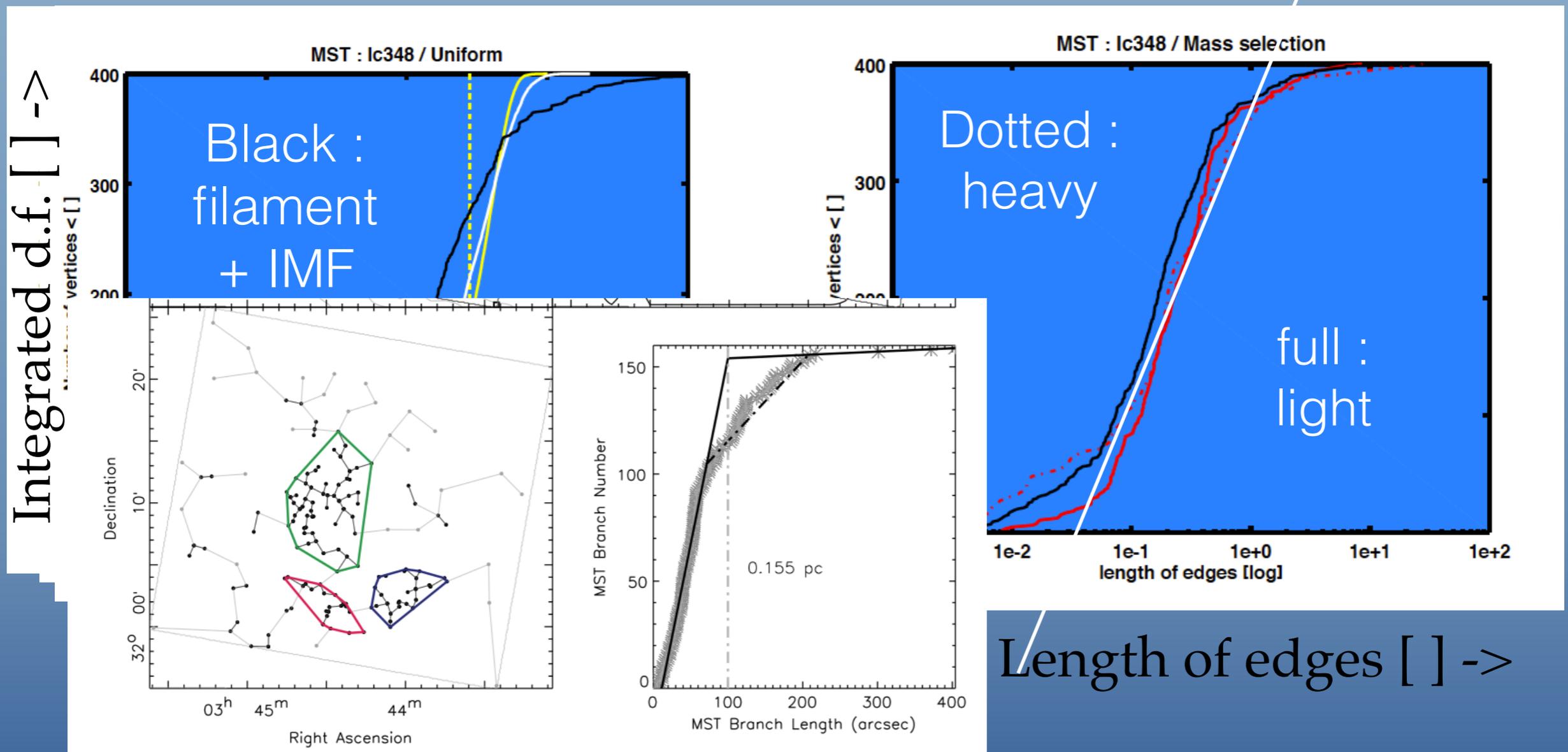
Integrated d.f. [] ->

Length of edges [] ->

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Different projection angles

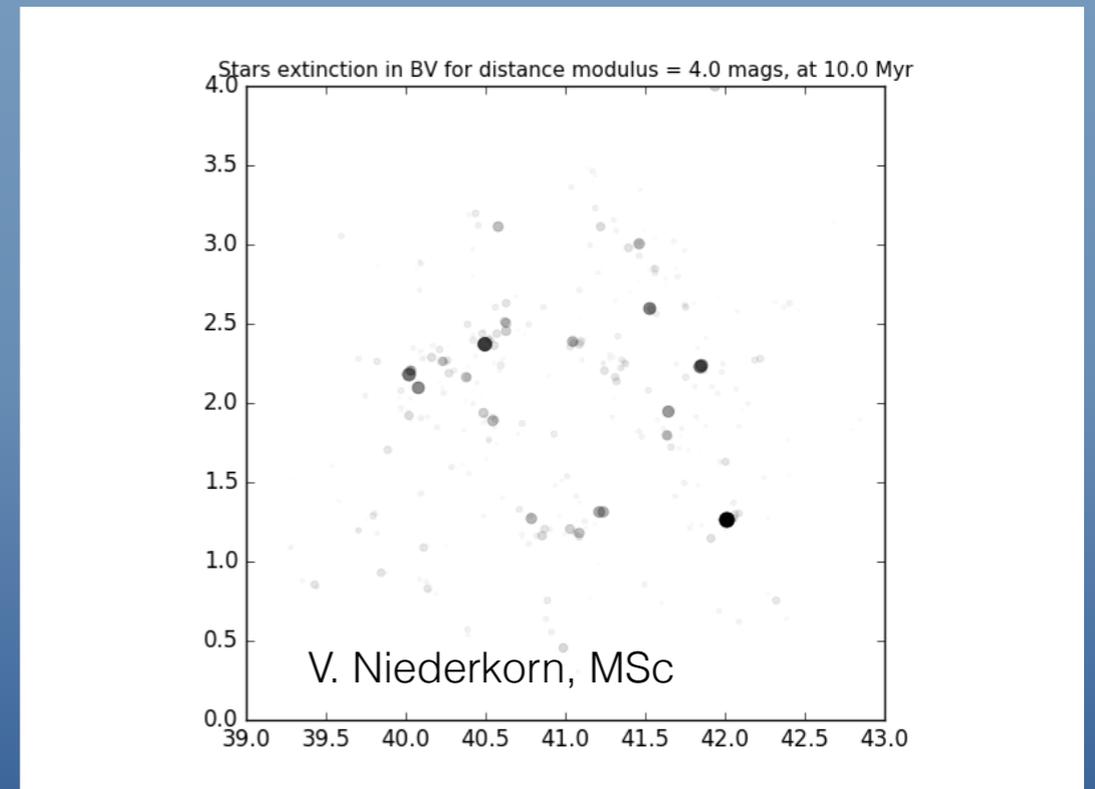
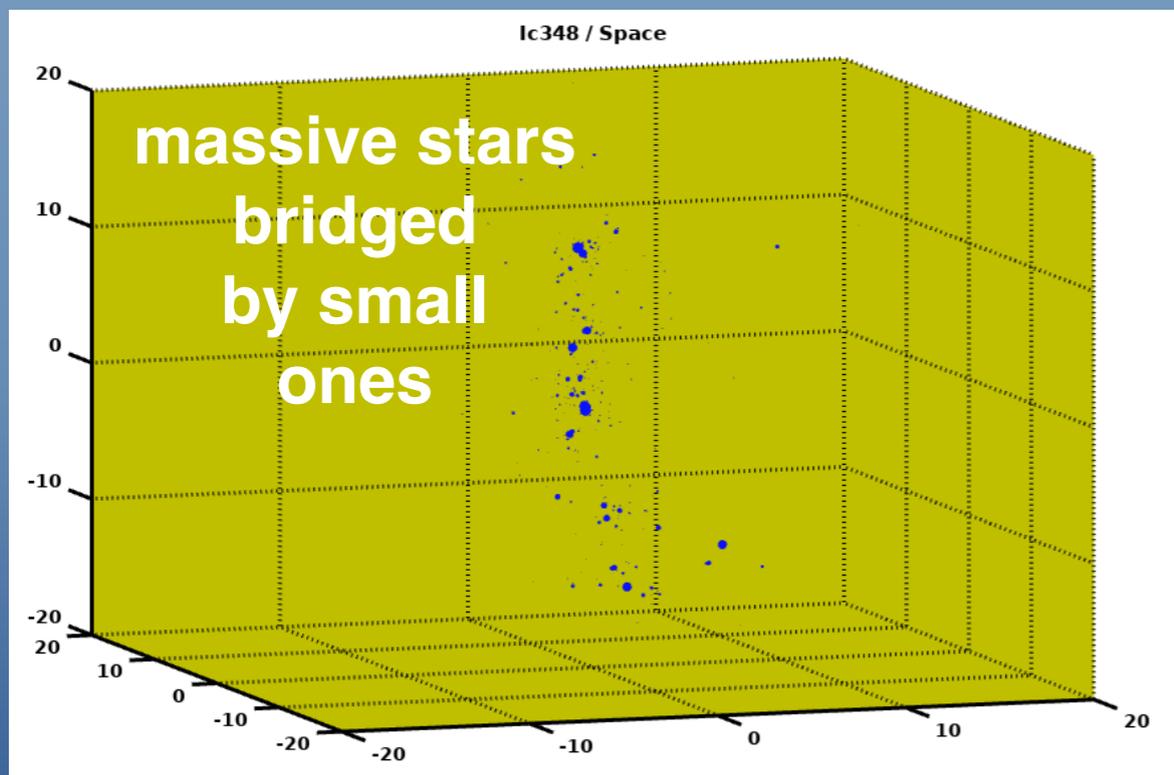
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Guthermut et al. 2009, ApJS

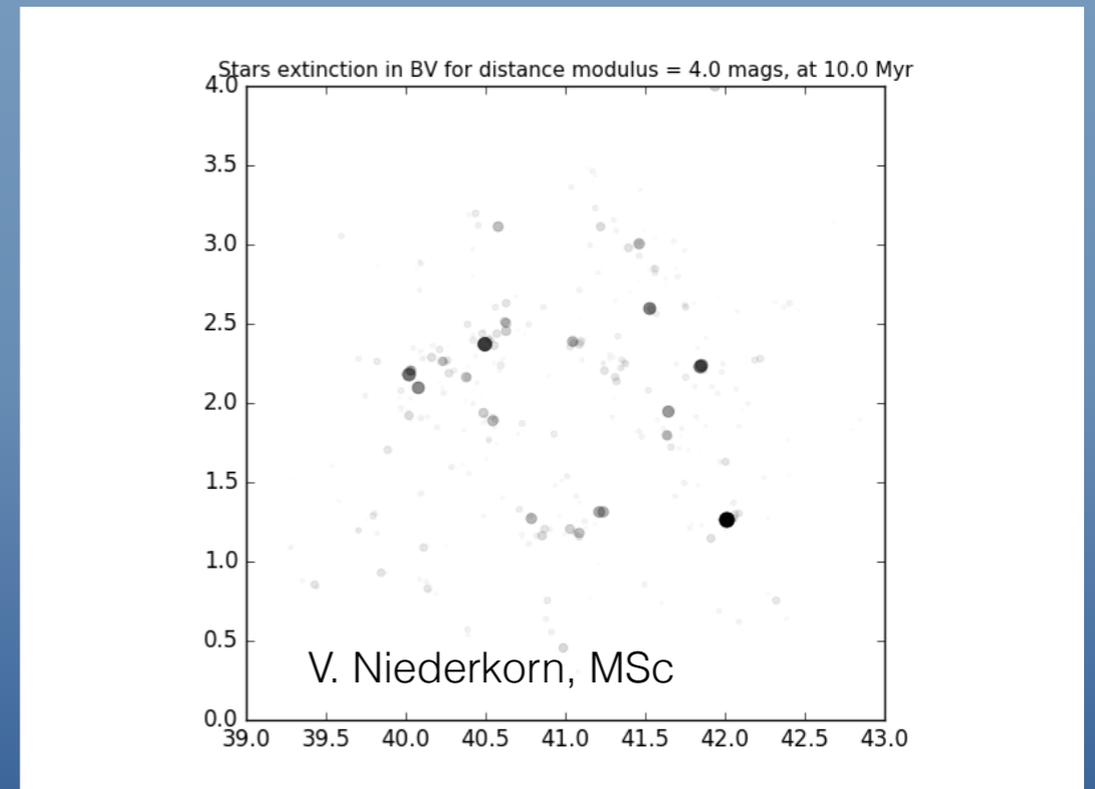
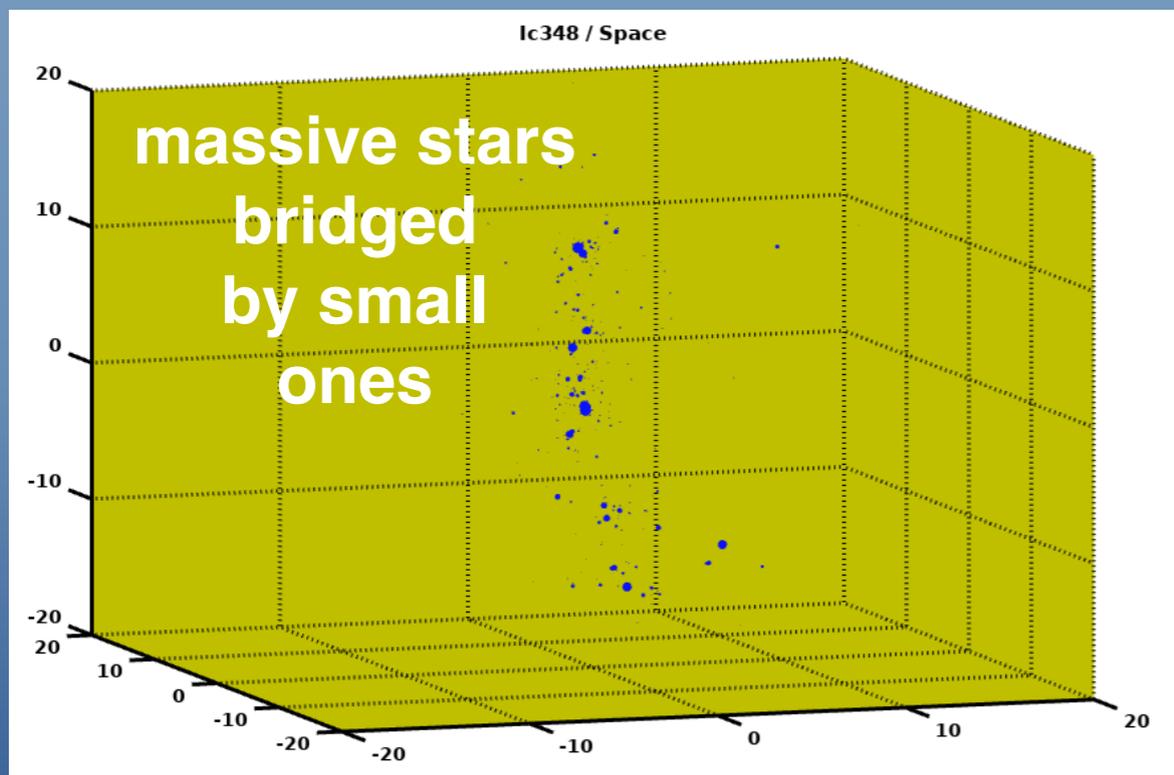
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- ◆ Explore the impact of extinction on the appearance of the skeleton



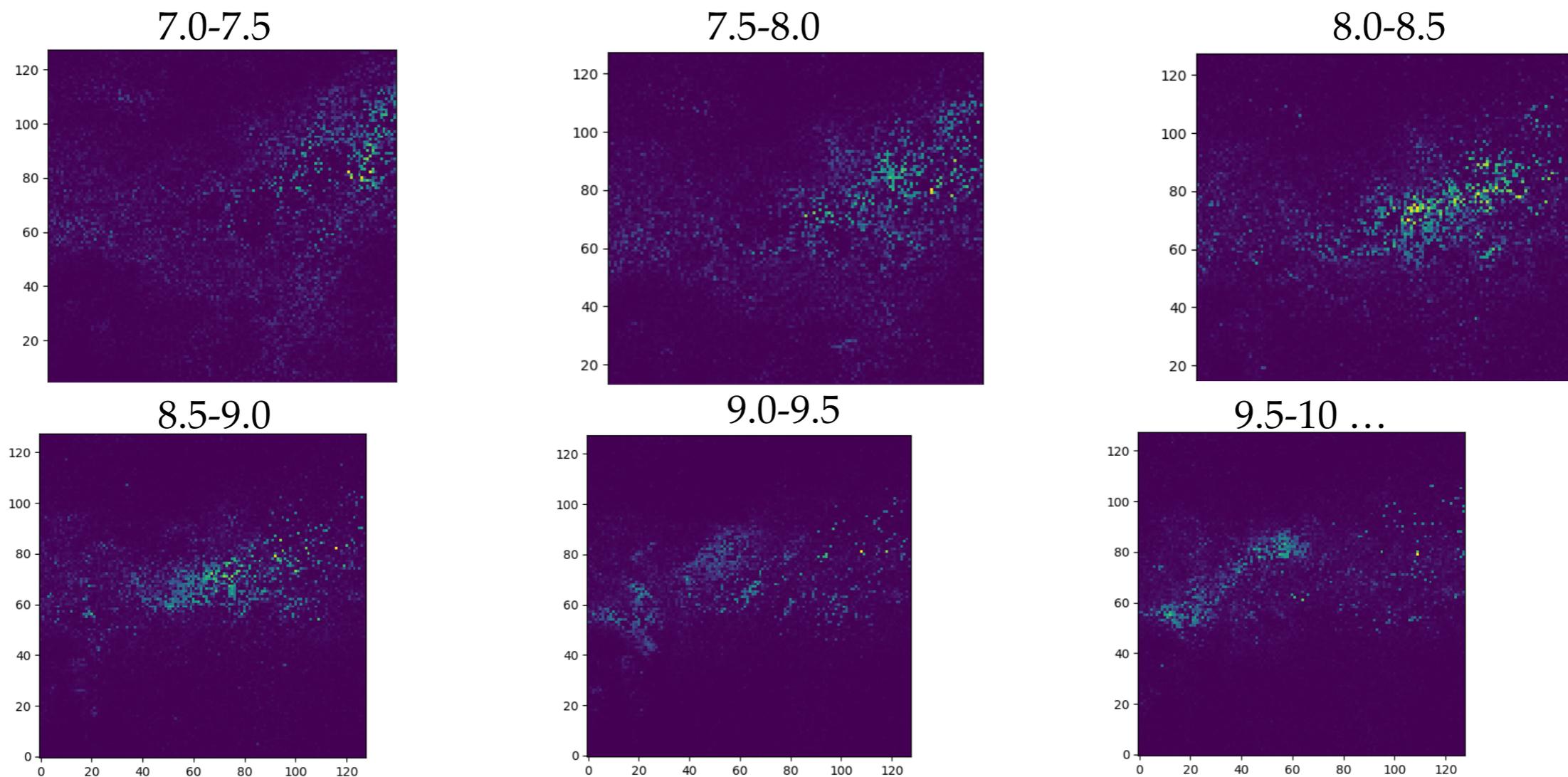
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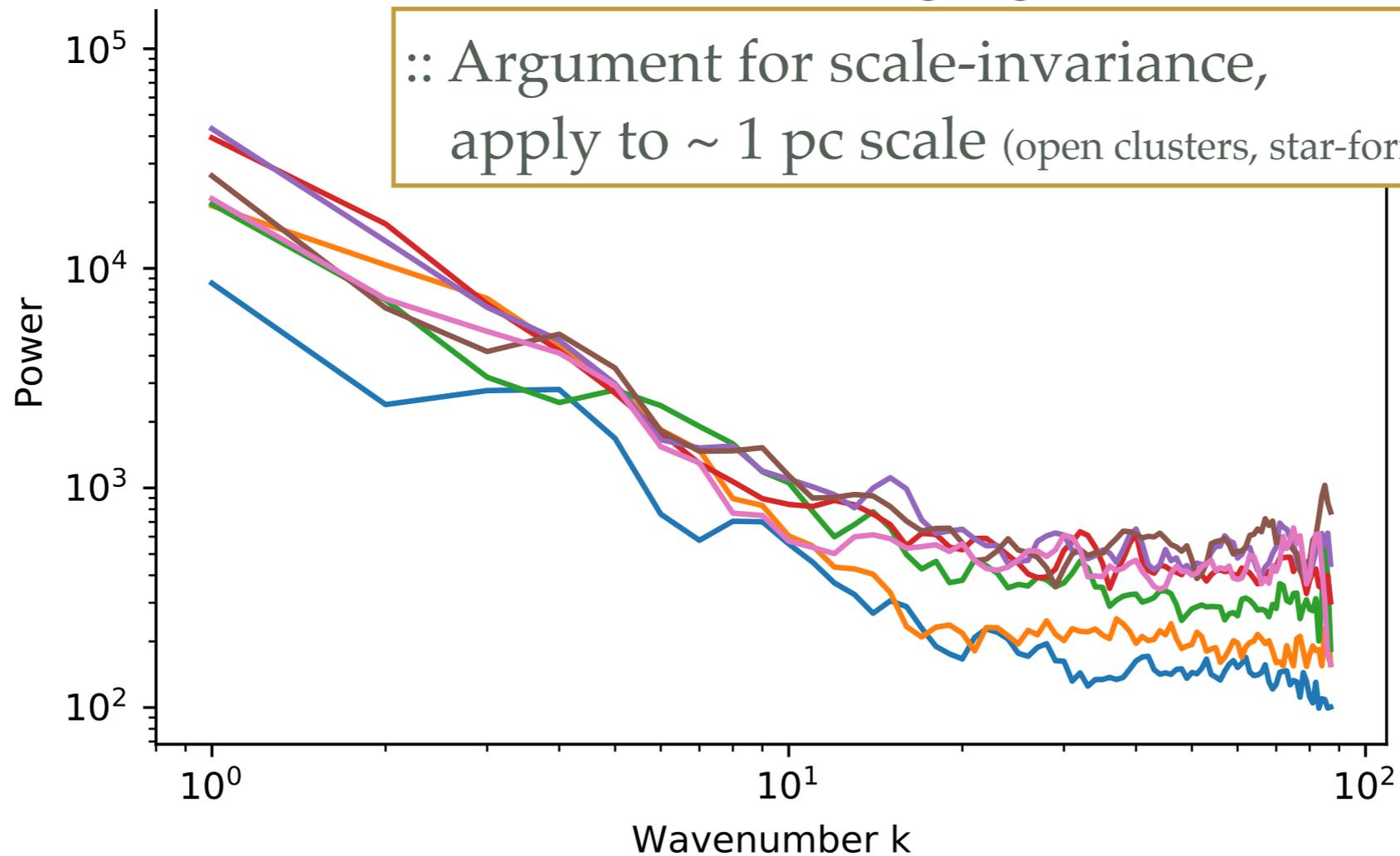
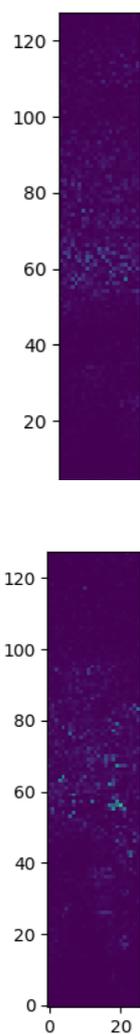
- ◆ Use the Pan-Starrs 1 extinction map (Green et al. 2015, ..)
- ◆ Set up maps at different distance scales (DM), same angular size



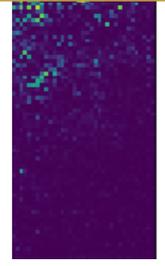
Exploring morphology using the Minimum Spanning Tree approach

◆ Use the Pan-Starrs 1 extinction map (Green et al. 2015, ..)

◆ Set FFT power spectrum : fixed direction on the sky, angular size distance modulus ranging form 7 to 11



:: Argument for scale-invariance, apply to ~ 1 pc scale (open clusters, star-forming regions, ..)

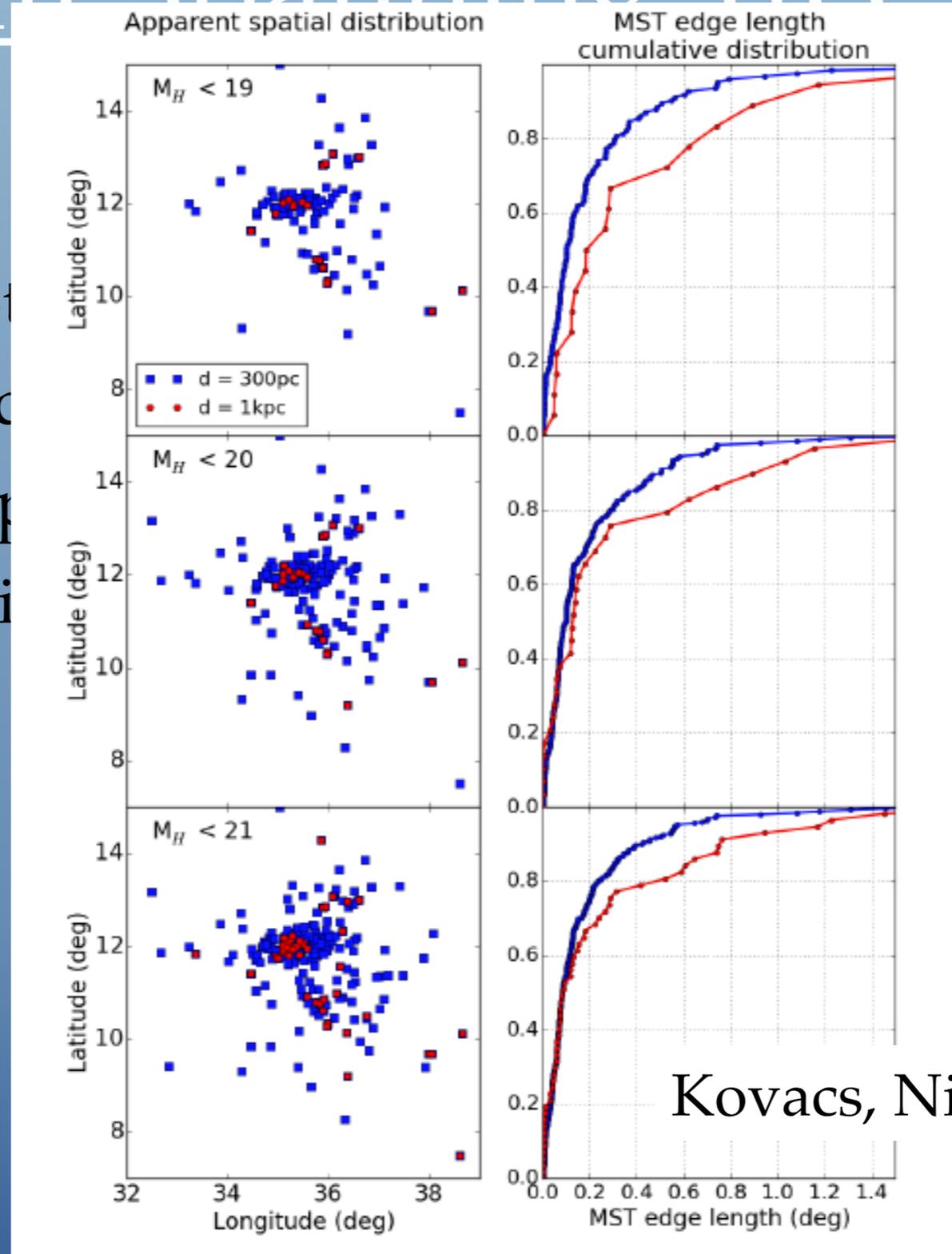


Exploring morphology using the Minimum Spanning Tree approach

- ◆ Morphology : apparent vs real .. selection, extinction
- ◆ Use the Pan-Starrs 1 extinction map (Green et al. 2015, ..)
- ◆ Extinction (= distance effect) : shift on MST statistics
- ◆ Set up a clump with $N \sim 400$ stars (e.g. Ic348)
- ◆ K-band extinction / bolometric correction : $\pm 20\%$ completeness @ $M_K = 21$

Exploring morphology using the Minimum Spanning Tree approach

- ◆ Morphology :
- ◆ Use the Pan-STARRS
- ◆ Extinction (= c
- ◆ Set up a clump
- ◆ K-band extinction
 $M_K = 21$



inction

al. 2015, ..)

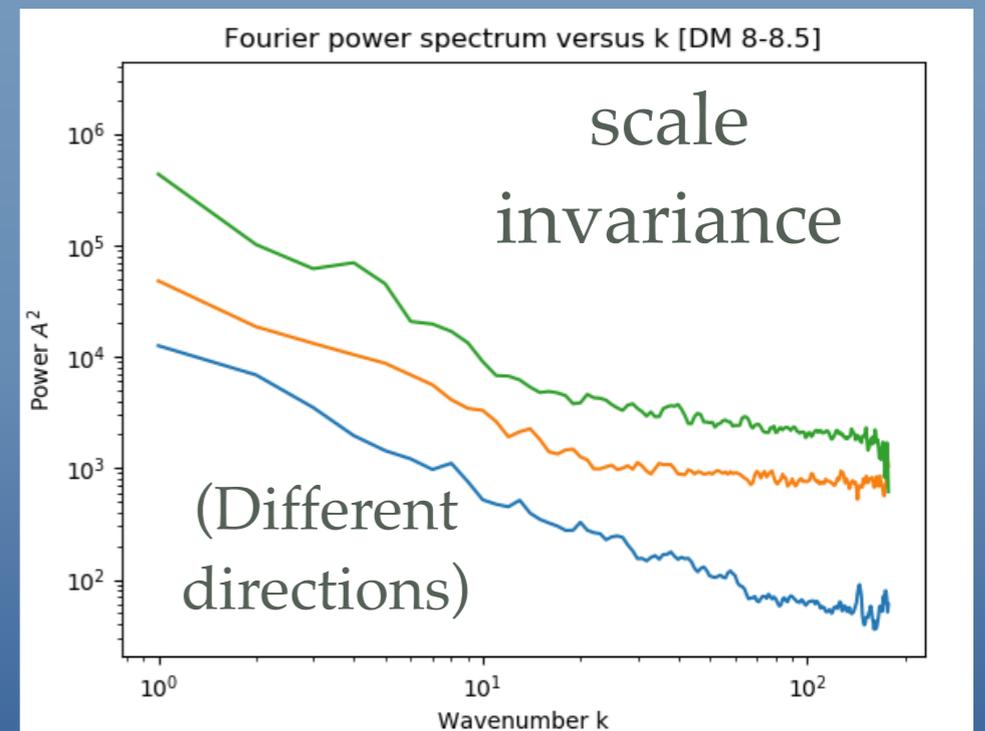
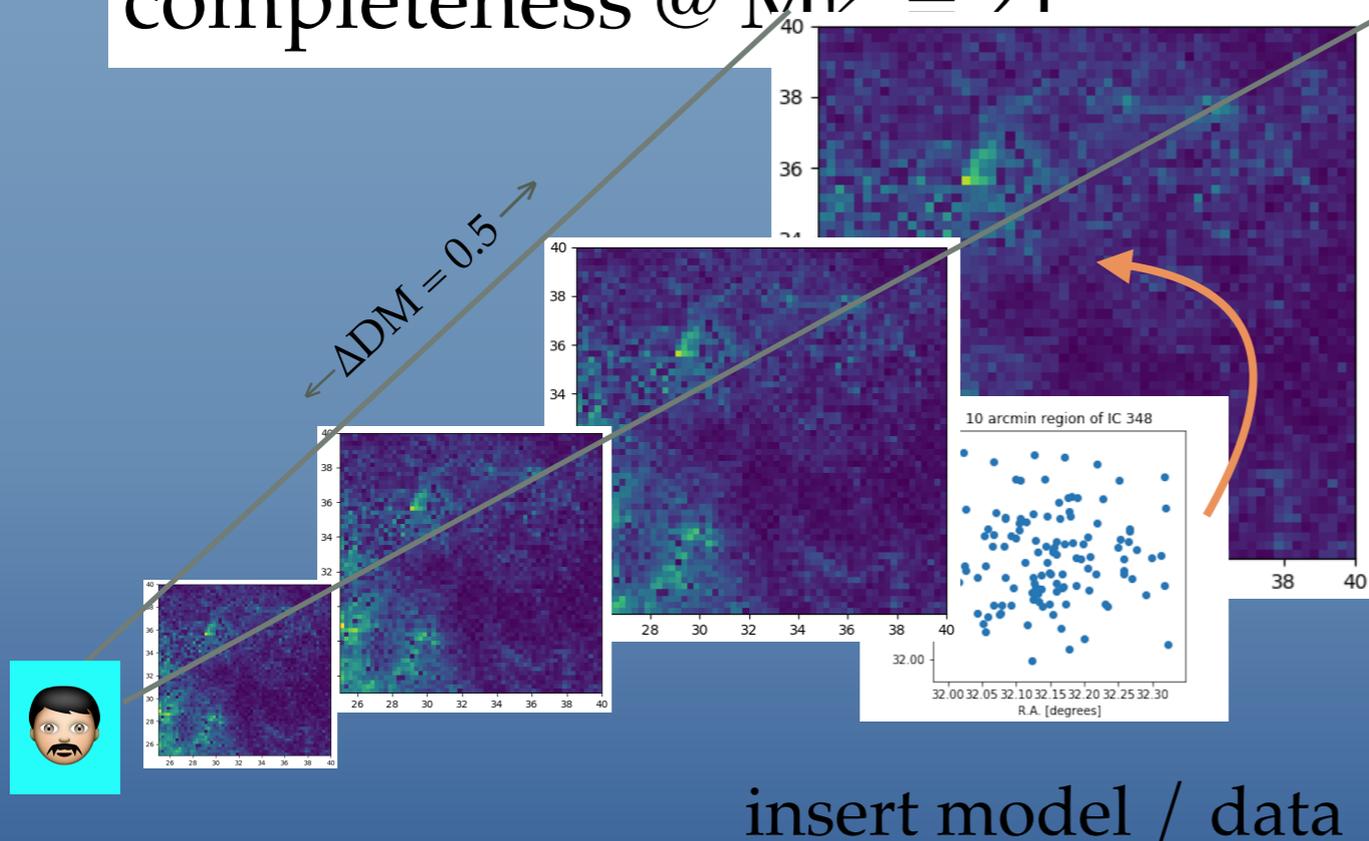
statistics

completeness @

Kovacs, Niederkorn, Dorval, ..

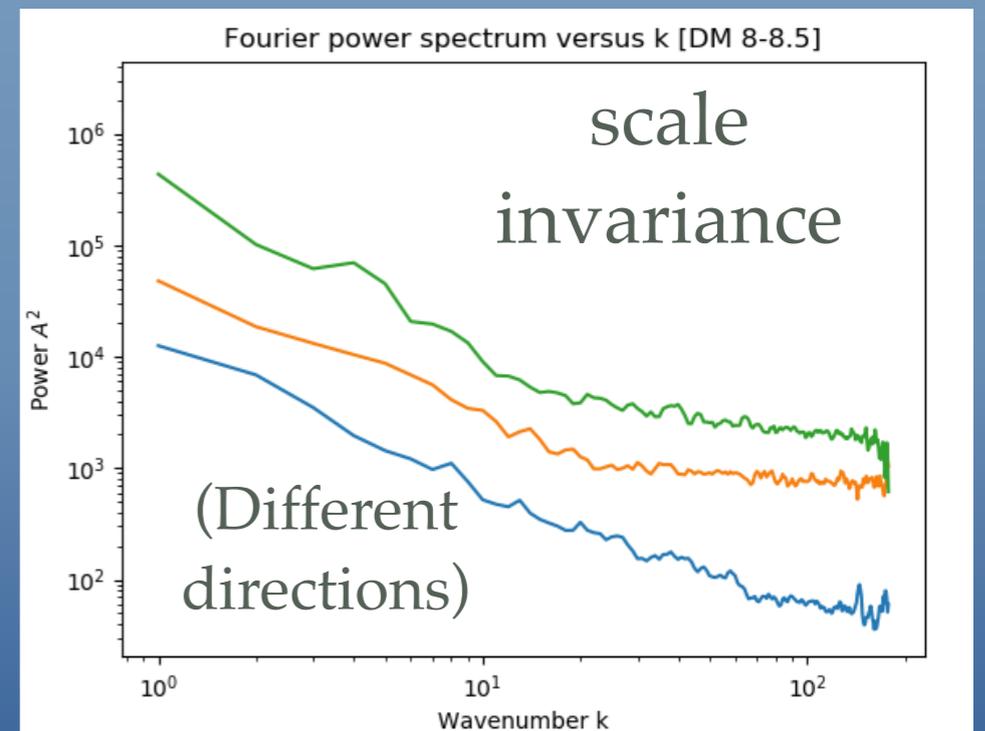
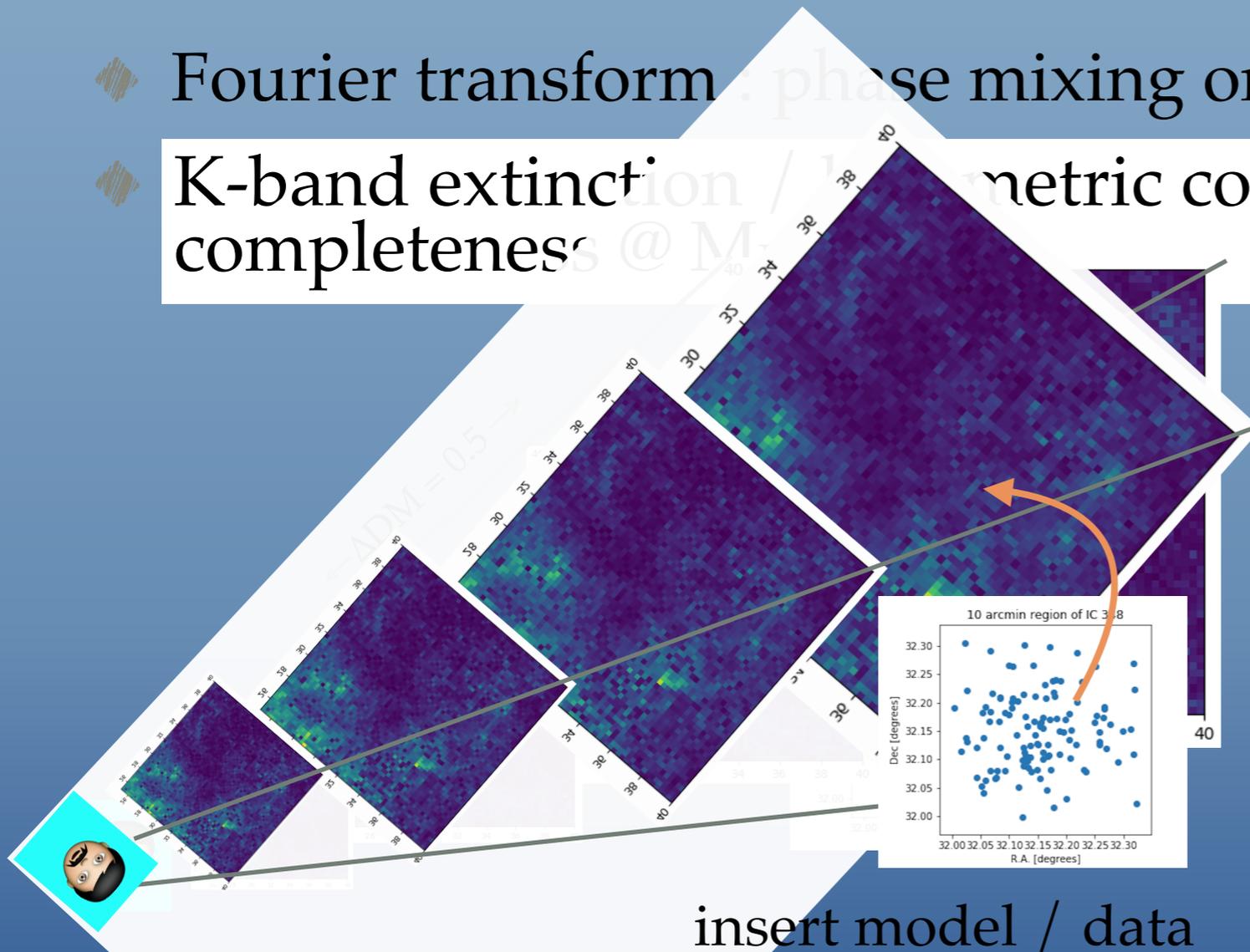
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- ◆ Use the Pan-Starrs 1 extinction map (Green et al. 2015, ..)
- ◆ Fourier transform : phase mixing on ~ 1 pc scale in ~ 1 Myrs
- ◆ K-band extinction / bolometric correction : $\pm 20\%$ completeness @ $M_{\text{IR}} = 21$



Exploring morphology using the Minimum Spanning Tree approach

- ◆ Morphology : apparent vs real .. selection, extinction
- ◆ Use the Pan-Starrs 1 extinction map (Green et al. 2015, ..)
- ◆ Fourier transform . phase mixing on ~ 1 pc scale in ~ 1 Myrs
- ◆ K-band extinction / A_K symmetric correction : $\pm 20\%$
completeness @ $M_K = 16$



Exploring morphology using the Minimum Spanning Tree approach

.. or not :

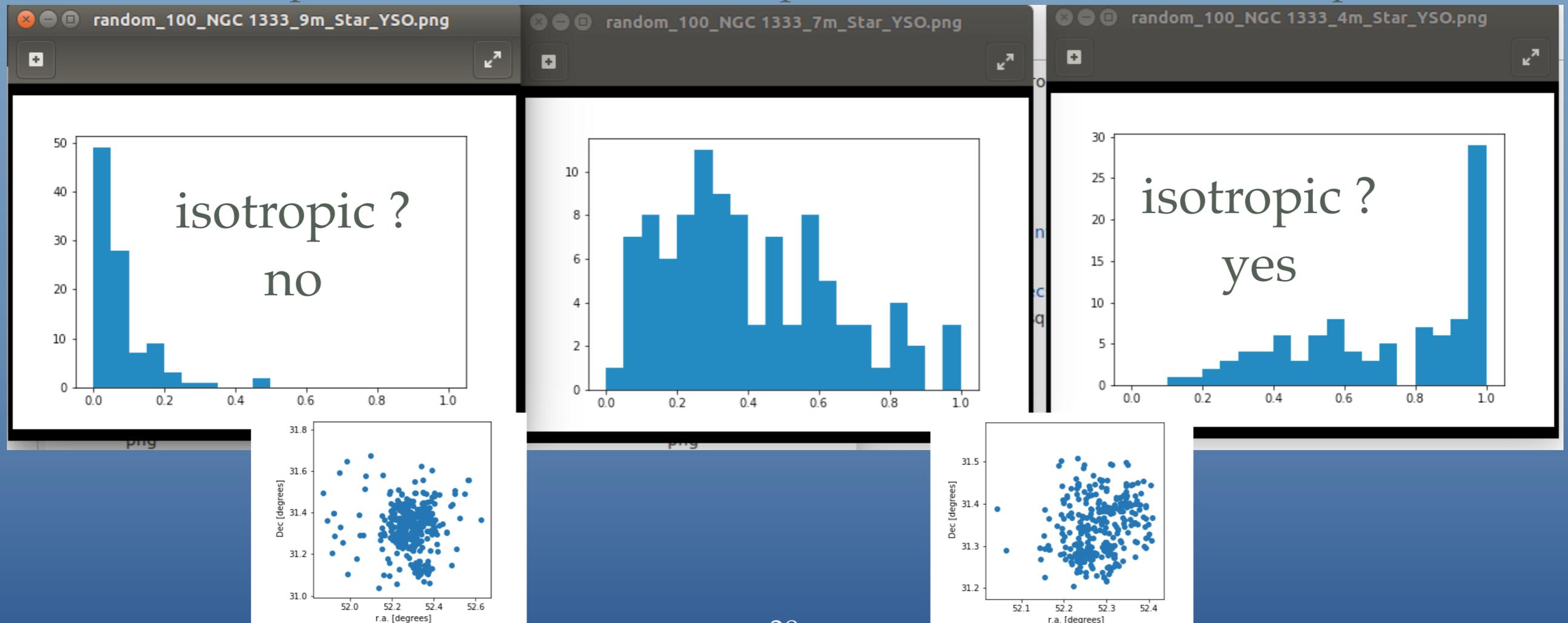
example of an Kolmogorov-Smirnov statistics applied to NGC 1333.

To do: compare actual clusters with embedded models

9 arcmin aperture

7 arcmin aperture

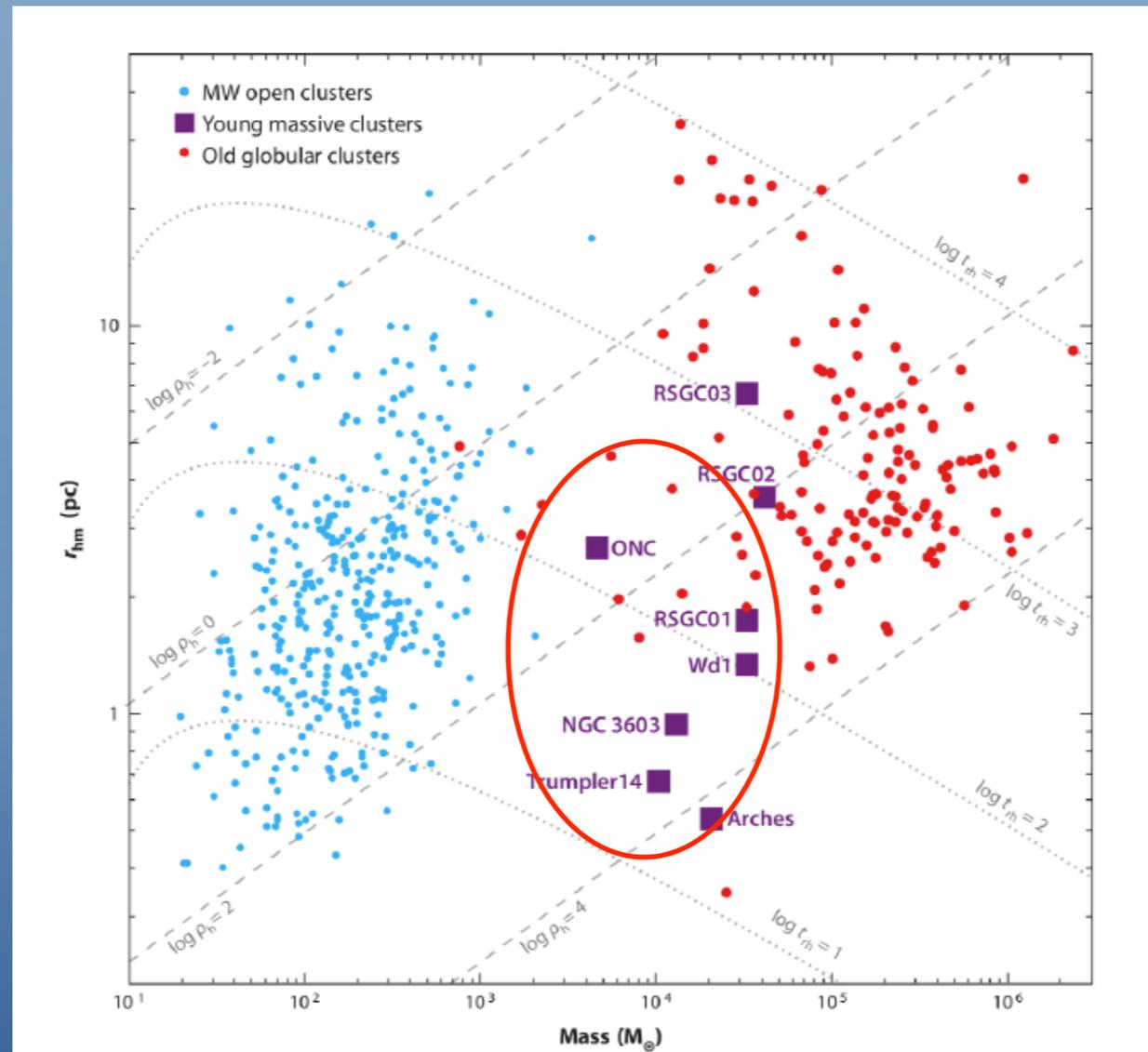
4 arcmin aperture



Exploring morphology

Orion (ONC), Wd1, ..

Possible multiple pops in ONC (de Marchi et al. 2017)
Un-relaxed embedded cores (Forster et al. 2015)



Integrated binary d.f. $F(-E)$: dynamical evolution, heating, disruption

- ◆ “Thermalised” equilibrium d.f. in binding energy $E = -G M\mu / a$

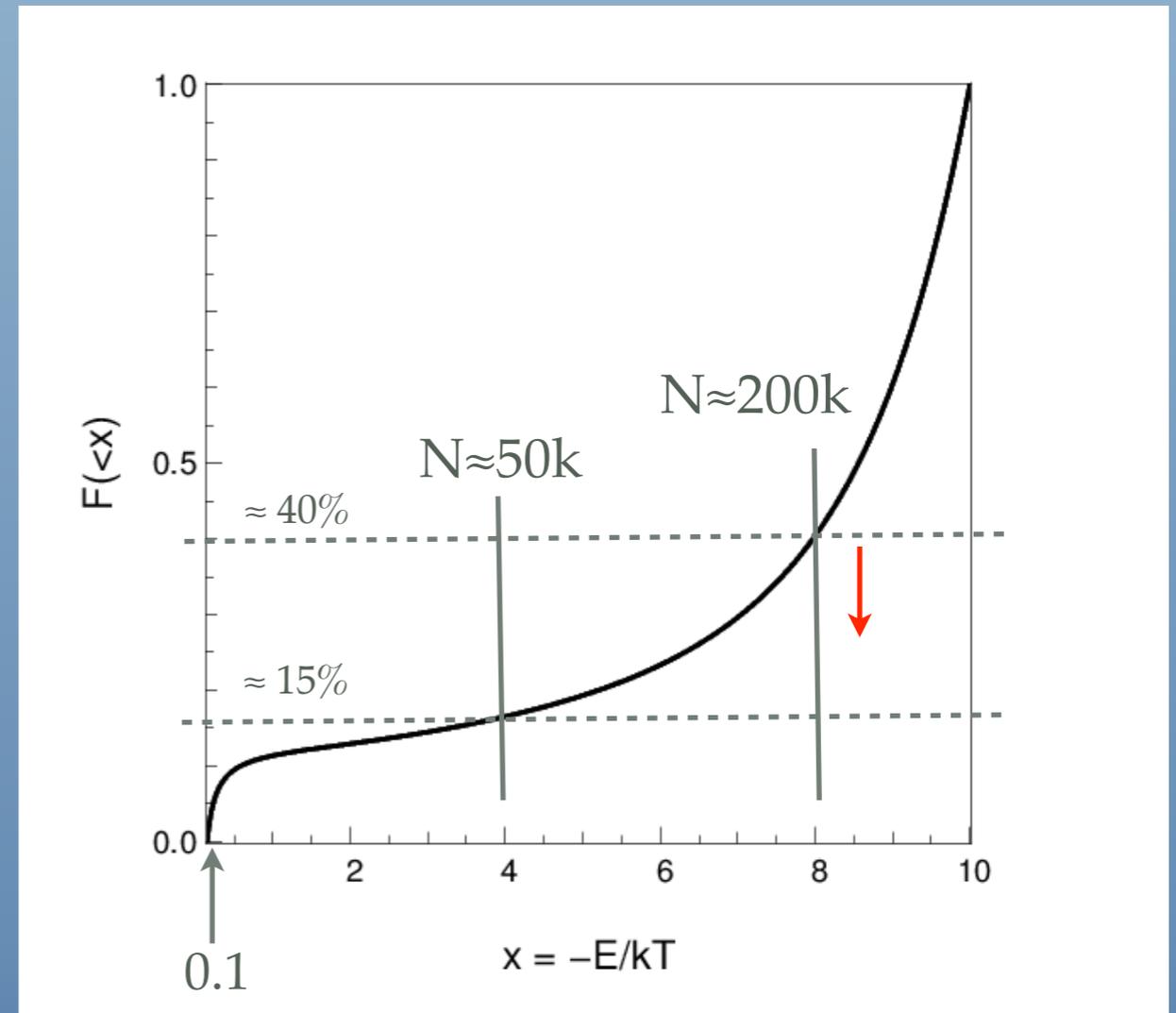
$$f(-E) = K \exp(-\beta E) / (-E)^{5/2}$$

- ◆ The Boltzmann factor

$$\beta = \frac{1}{k_{\beta} T} = \frac{1}{\frac{1}{2} m \sigma^2}$$

- ◆ The fraction of binaries heated at formation time scales with \sqrt{N} , the number of (proto) stars formed

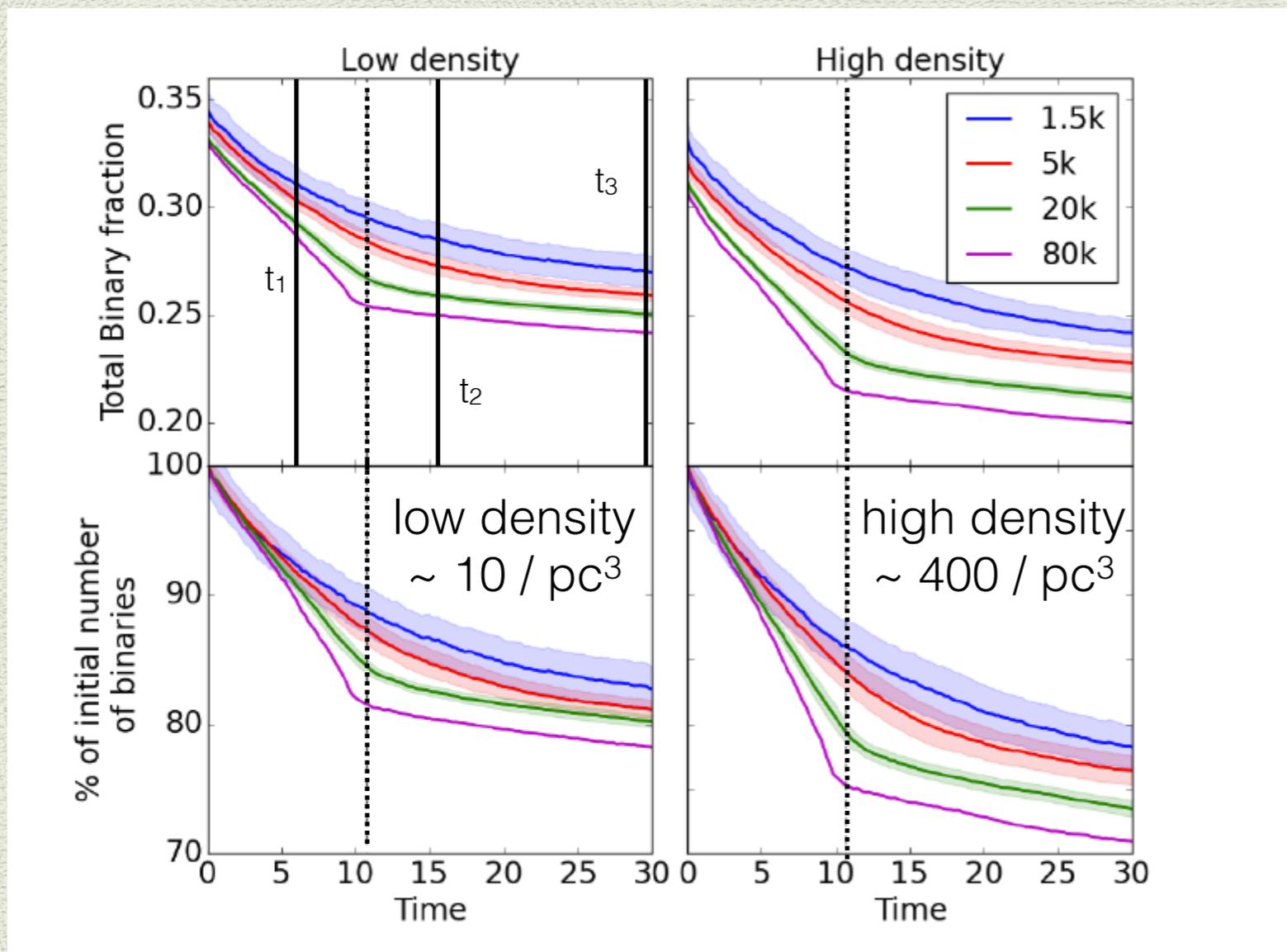
$$\frac{\delta W}{k_{\beta} T} \simeq \frac{25\pi}{4} \sqrt{\frac{5}{6}} \times 10^{-5} \frac{a_{bin}[AU]}{R_o[0.5pc]} \sqrt{N}$$



Lower-limit on R_o

Stellar clumps:

Internal dynamics of multiple stars significant



Evolution up to global mixing / relaxation

t_1 : internally, clumps
dotted : violent in-fall
 t_2 : mixing (~ 1 Myr)
 t_3 : end (~ 4 Myr)

Processing of binary stars
for models
with different N but same
IMF + binary population

:: Survival rate weakly dependent on N,
sharp transition at the bounce ($t = \text{dots}$)

cf. Dorval PhD + et al. 2017

Stellar clumps:

Internal dynamics of multiple stars significant

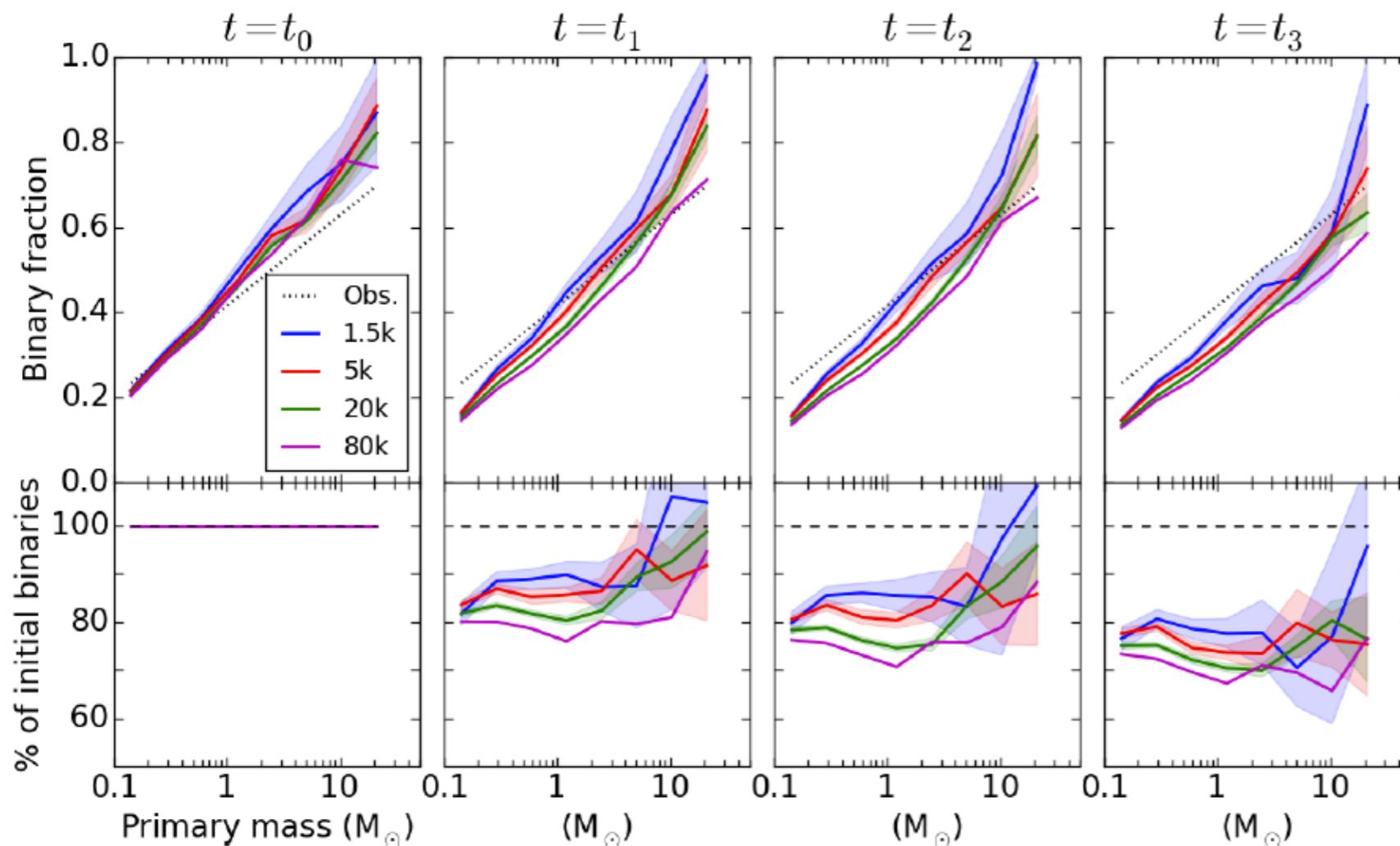


Figure 7.4: Same key as Fig. 7.3. The data are from high density models.

Processing of
binary stars
less severe
in
open clusters
(heavy primaries)

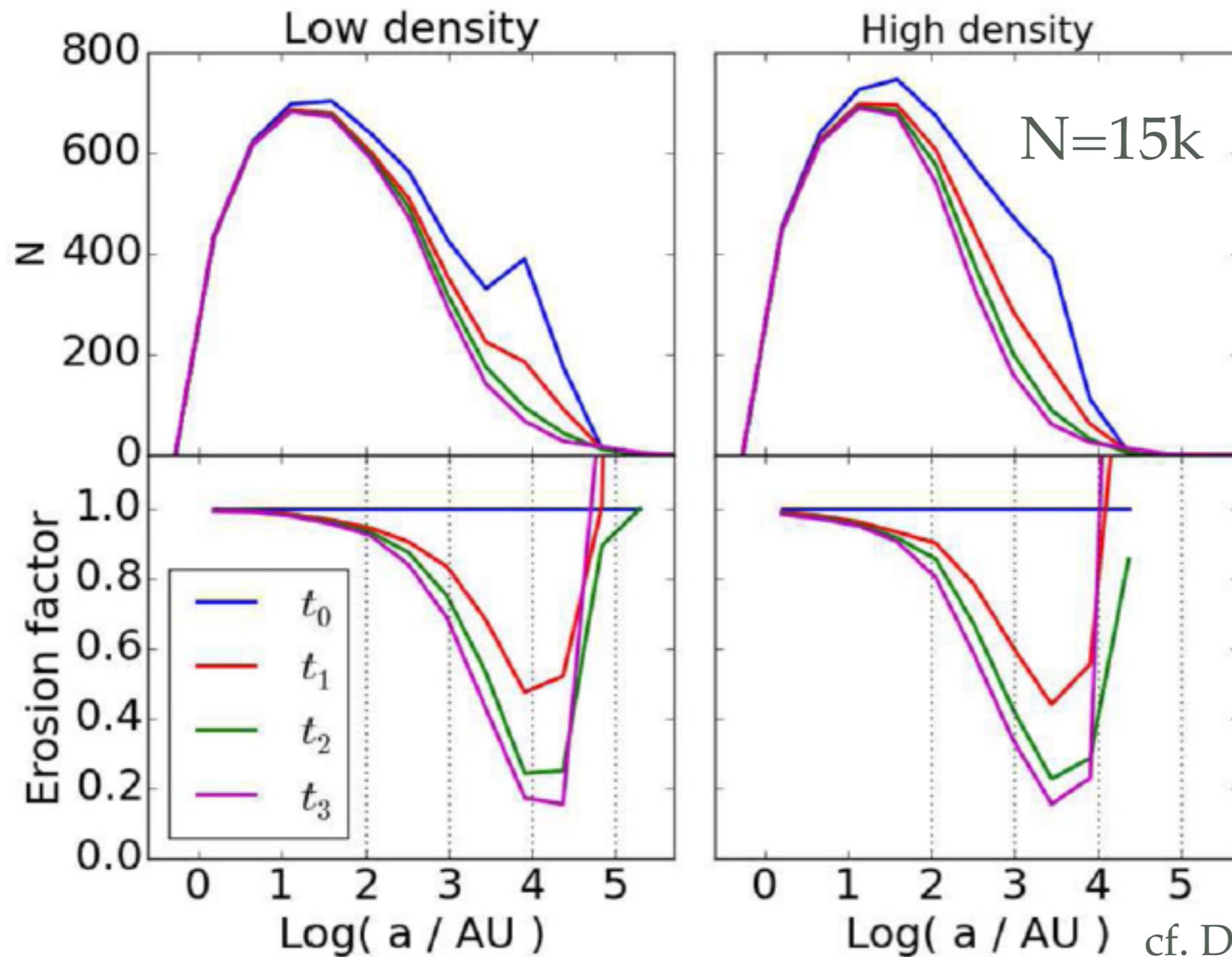
:: different dissolution rates wrt to primary mass

Erosion @ la
Marks-Kroupa (2011,12)
Collusion @ la
Kouwenhoven et al (2010)

cf. Dorval PhD + et al. 2017

Stellar clumps:

Internal dynamics of multiple stars significant



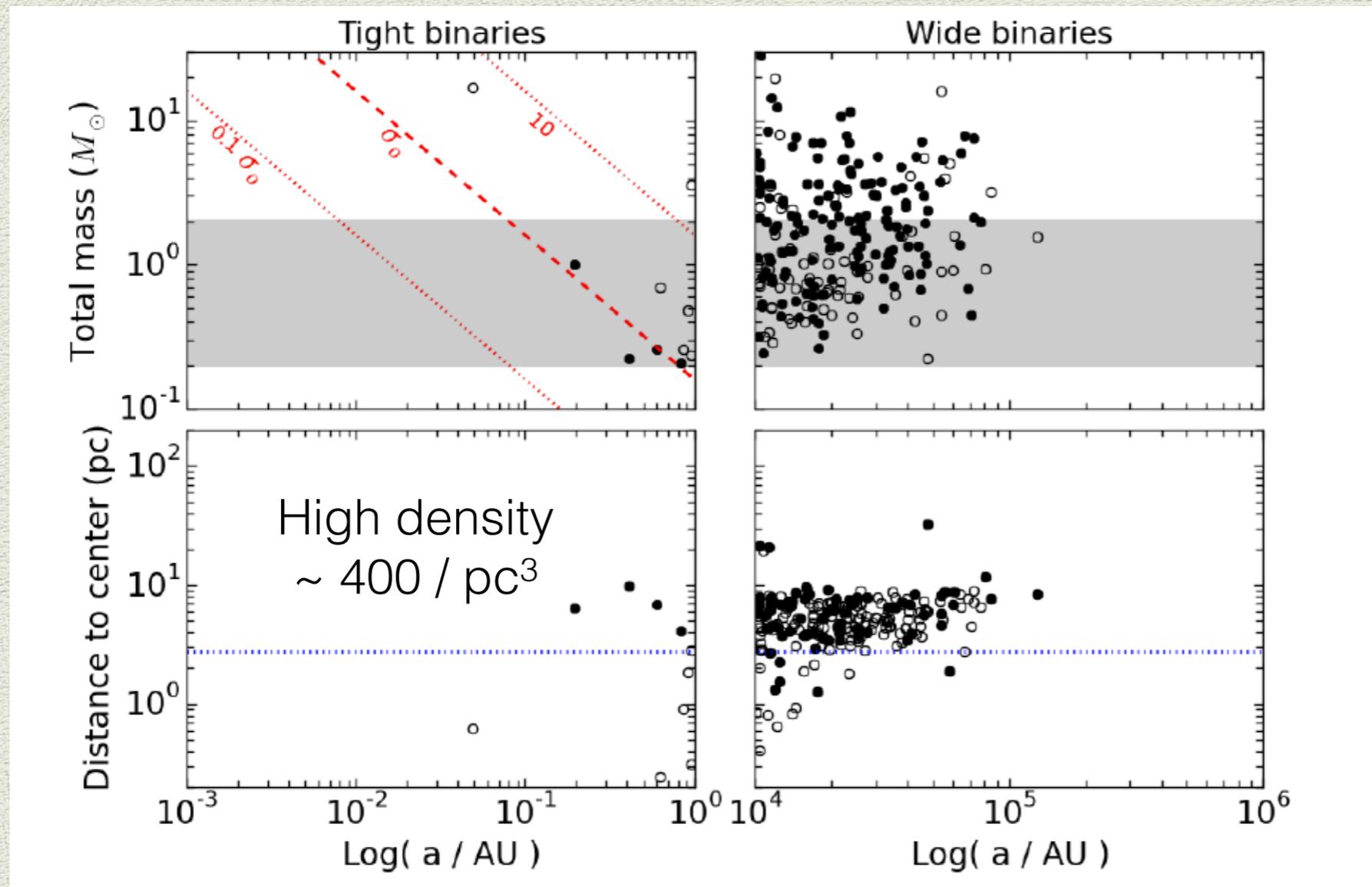
Processing of
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cf. Dorval PhD + et al. 2017

Stellar clumps:

The formation of tight binaries linked to environment



Exchange
takes place
within clumps
"time allowing"
cf. Leigh & Geller 2015

The formation of
tight binaries by
binary-binary
exchange collisions
linked directly to
the global mean
density !

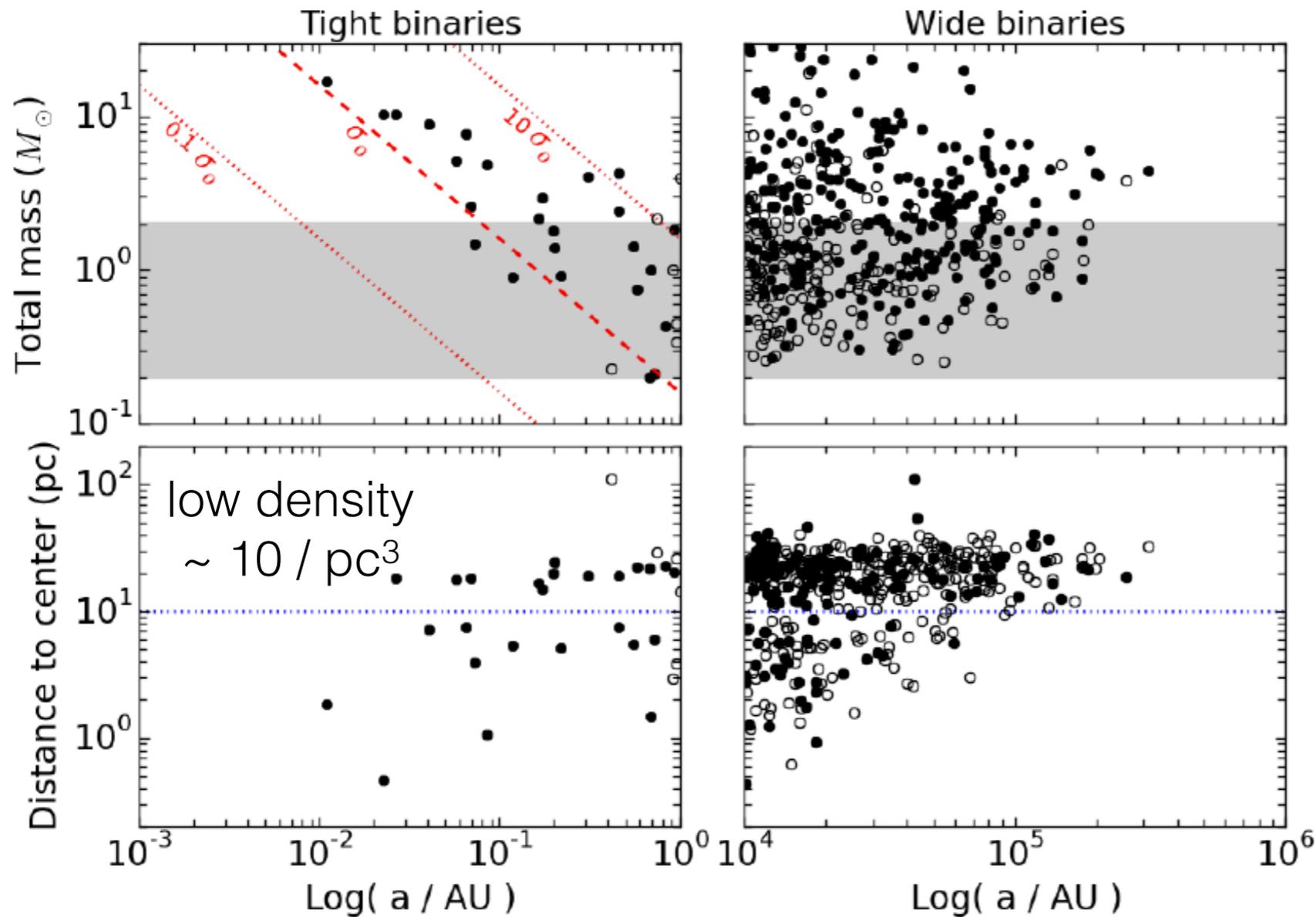
:: Collision rate for destruction

When $\theta > 100$: gravitational focusing important

$$\begin{aligned} \tau_{\text{coll}}^{-1} &= 16\sqrt{\pi}n\sigma a^2\theta \\ &= 8 \times 10^{-4} \text{ Myr}^{-1} \left(\frac{n}{700\text{pc}^{-3}} \right) \left(\frac{0.5\text{km.s}^{-1}}{\sigma} \right) \left(\frac{a}{\text{AU}} \right) \left(\frac{M}{2M_{\odot}} \right) \end{aligned}$$

Stellar clumps:

The formation of tight binaries linked to environment



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Summary

- Young clusters (open, rich) start out with odd geometry and sub-virial global velocities
- They should mix quickly yet have time to form stars first ..
- The stellar clumps are top-heavy with respect to field stars ;
- Outflows lead to wide-binaries forming [:: phase-space correlations]
- bi-bi exchanges + tight binaries favoured in low-density environment [:: amplification by gravitational focusing]
- surrounding gas may yet lead to isolated tight binaries merging
- Extinction maps scaled down to map out the low-mass stars, explore morphology, dynamics